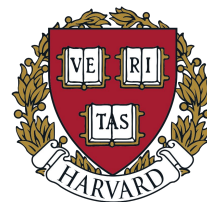


# Superposed Decoding



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NeurIPS 2024.

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# Drafting Scenarios

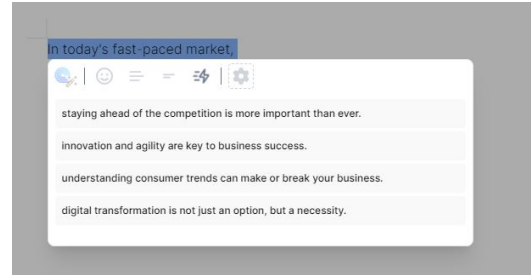
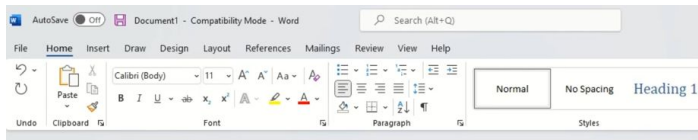
- Users often want multiple distinct outputs from LLMs



```
const express = require('express');
const app = express();
const port = process.env.PORT || '8080';

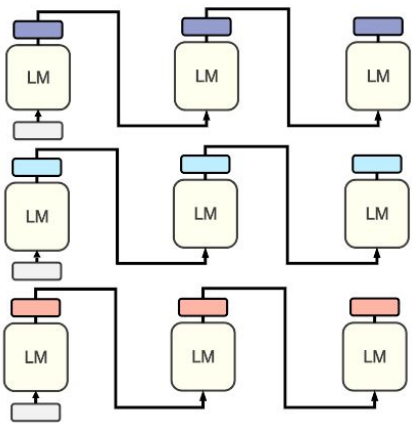
app.get('/', (req, res) => {
  res.send('hello tabnine');
})

app.listen(port, () => {
  console.log('Listening at port %s', port);
  console.log('Listening at port: ' + port);
  console.log('Listening at port');
  console.log(port);
  console.log('Listening on port %');
  confirm
  console
  const
  continue
})
```



# Current Approaches

- Decoding Methods
  - Nucleus Sampling
  - Beam Search
  - Top-k Sampling
  - Greedy Decoding (Only one draft)
- **Multiple inference passes** (batch size = 1)



"I just arrived in Xalapa, Mexico - today was my first"

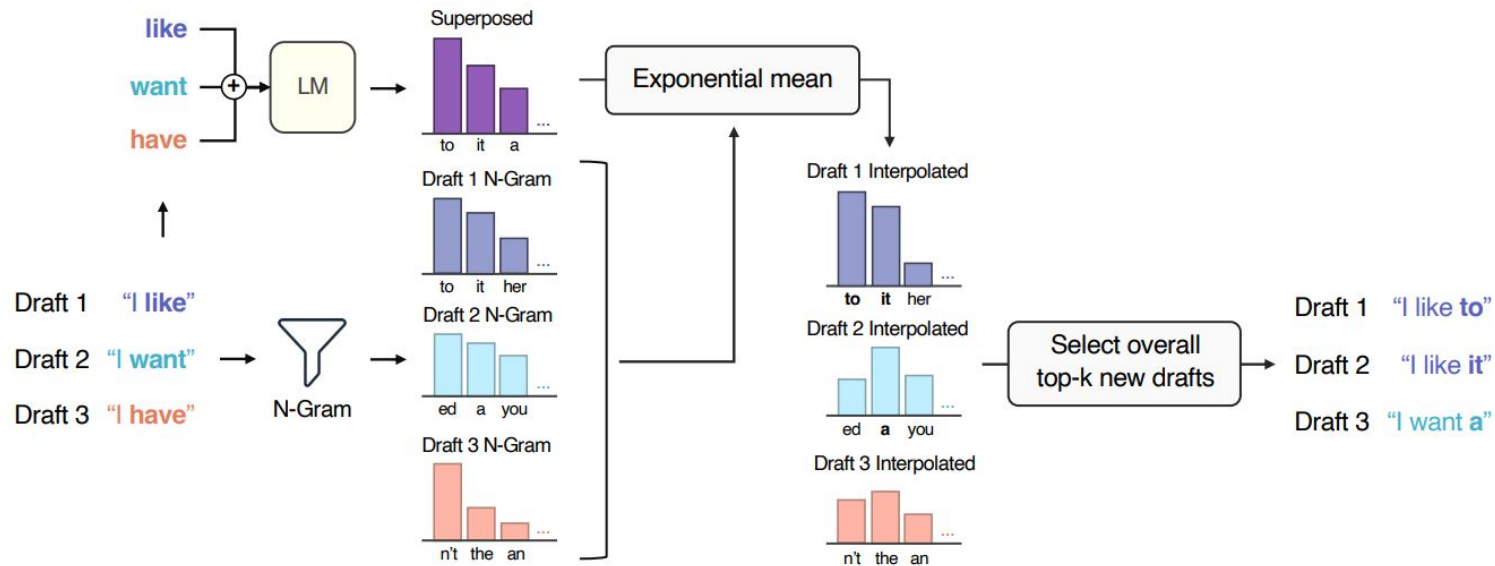


day of class. At Universidad Veracruz...  
day of the Rosenkranz School at the...  
day of orientation, and I could not wait to...



# Superposed Decoding (SPD)

Idea: Linearly combine token embeddings to extend all  $k$  drafts with **one** inference pass



# First Timestep

1. Let  $x$  denote token in vocabulary  $V$  and  $M=(x_1, \dots, x_m)$  an initial prefix of  $m$  tokens.

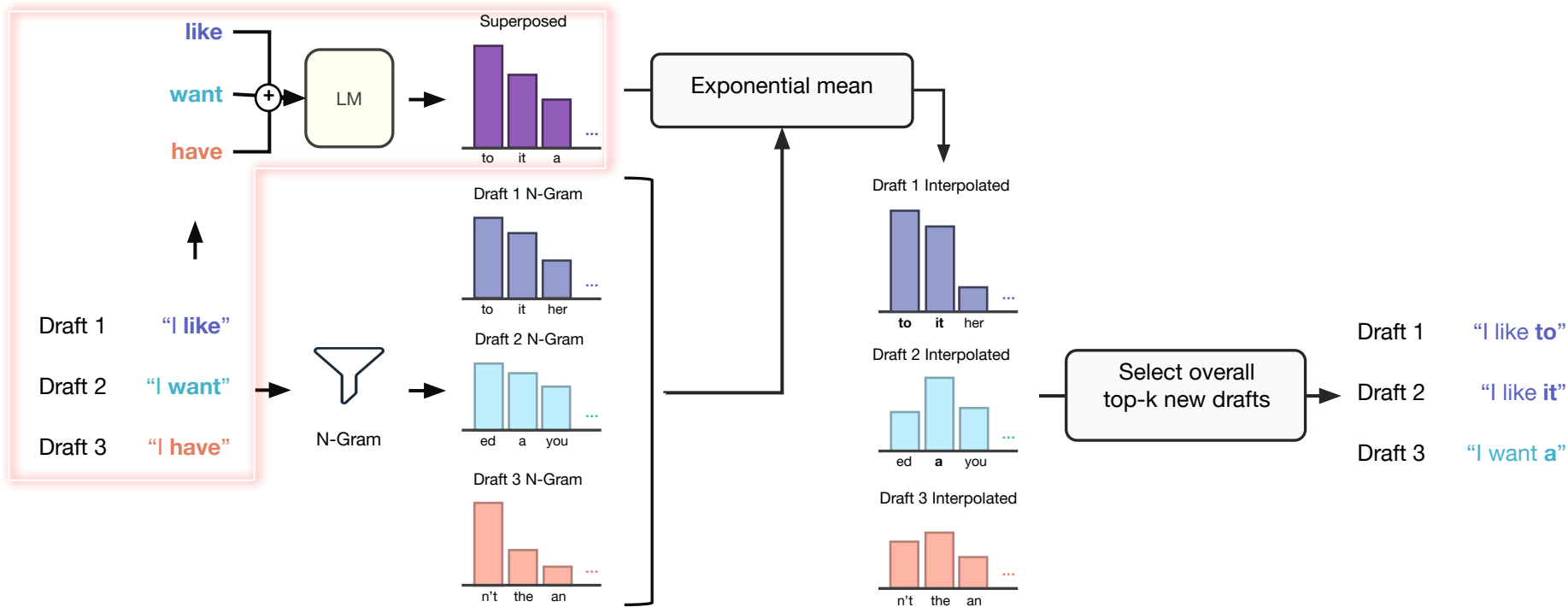
2. Grow initial drafts using model  $\theta$ :

Draft 1 “|”      Draft 1 “| like”

Draft 2 “|”    →    Draft 2 “| want”

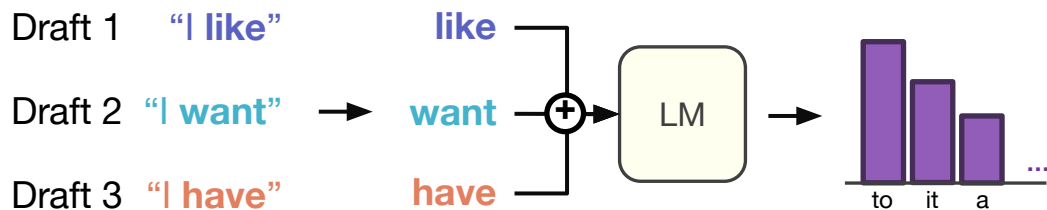
Draft 3 “|”      Draft 3 “| have”

# Step 1: Superposed Embedding Inference



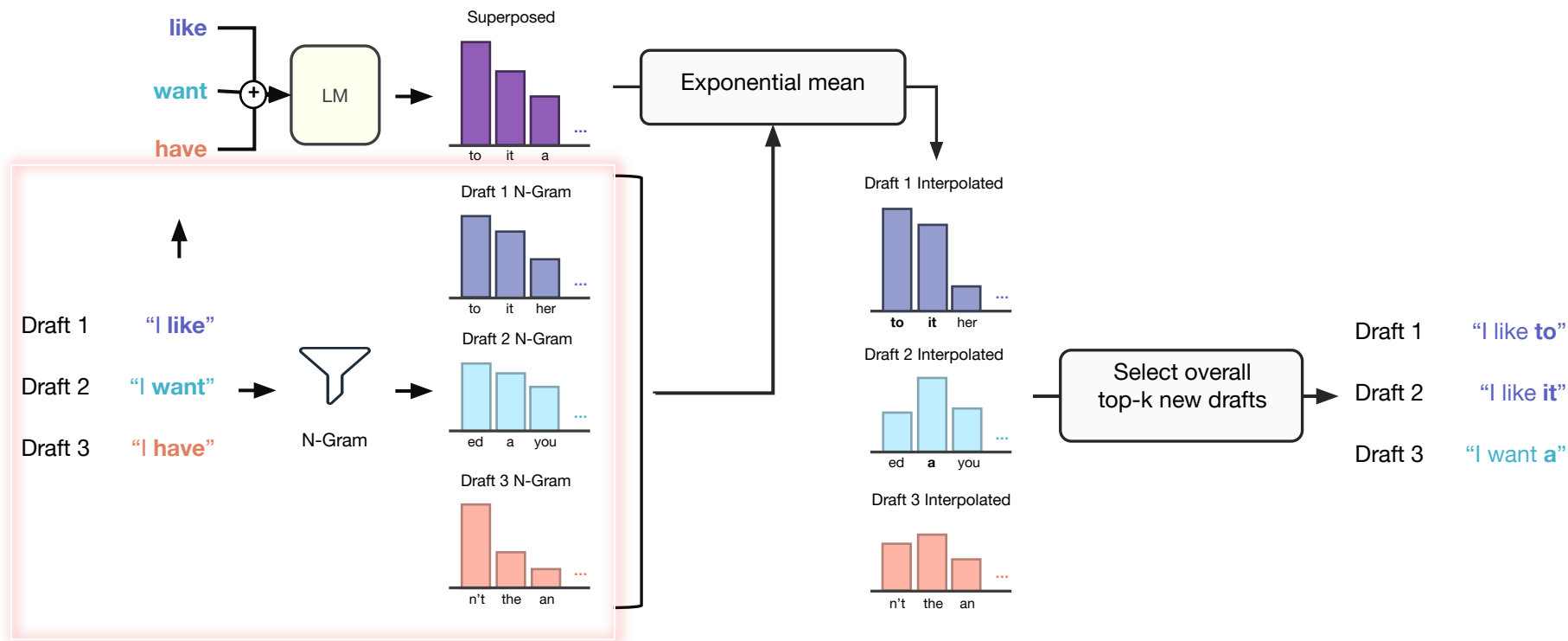
# Step 1: Superposed Embedding Inference

- Find weighted combination of the embeddings of each draft's most recent token.



- Truncate the resulting distribution to only the top  $k$  tokens.

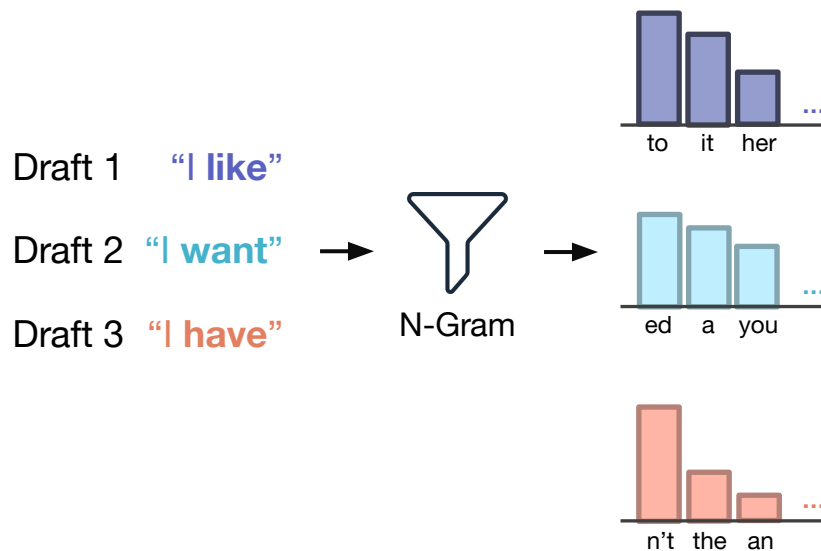
# Step 2: N-Gram Distribution



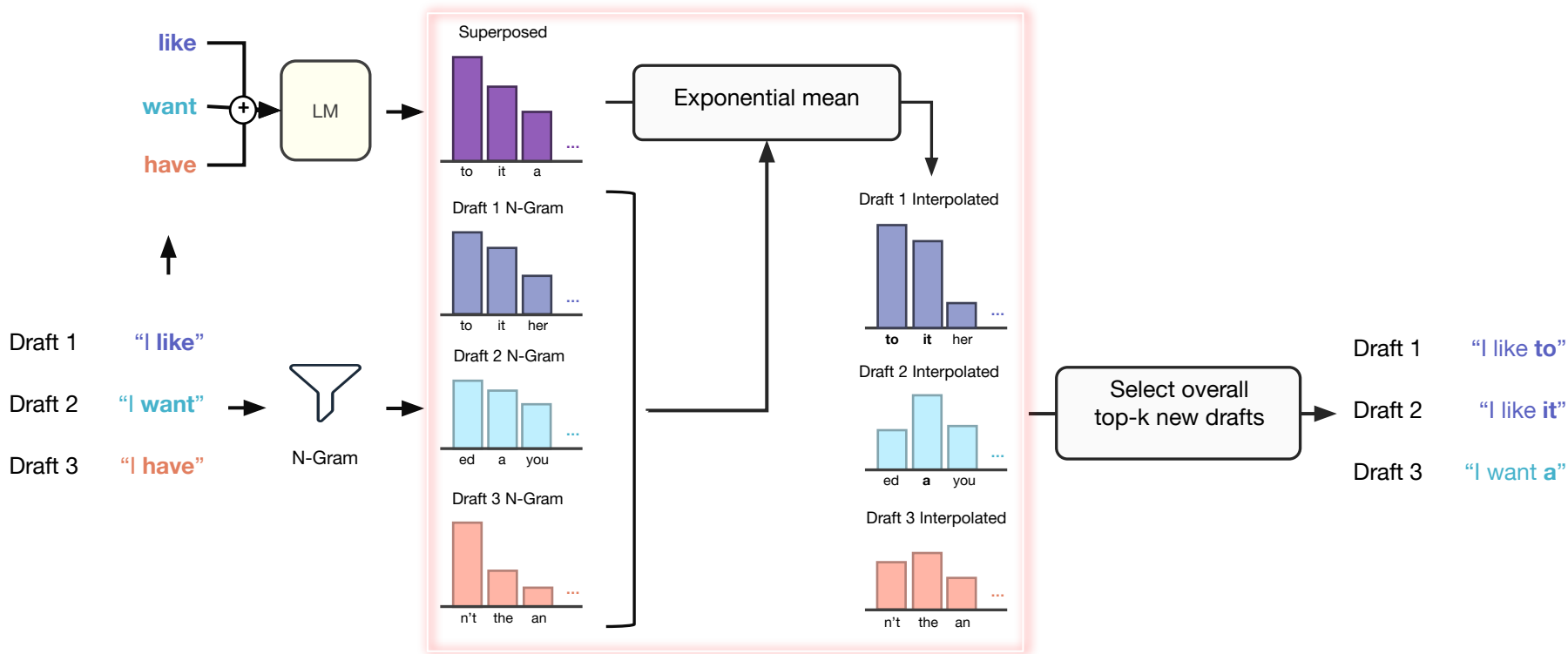


## Step 2: N-Gram Distribution

- Interpolate the next token distributions from a set of  $n$ -gram models ( $n \in [2, 6]$ )

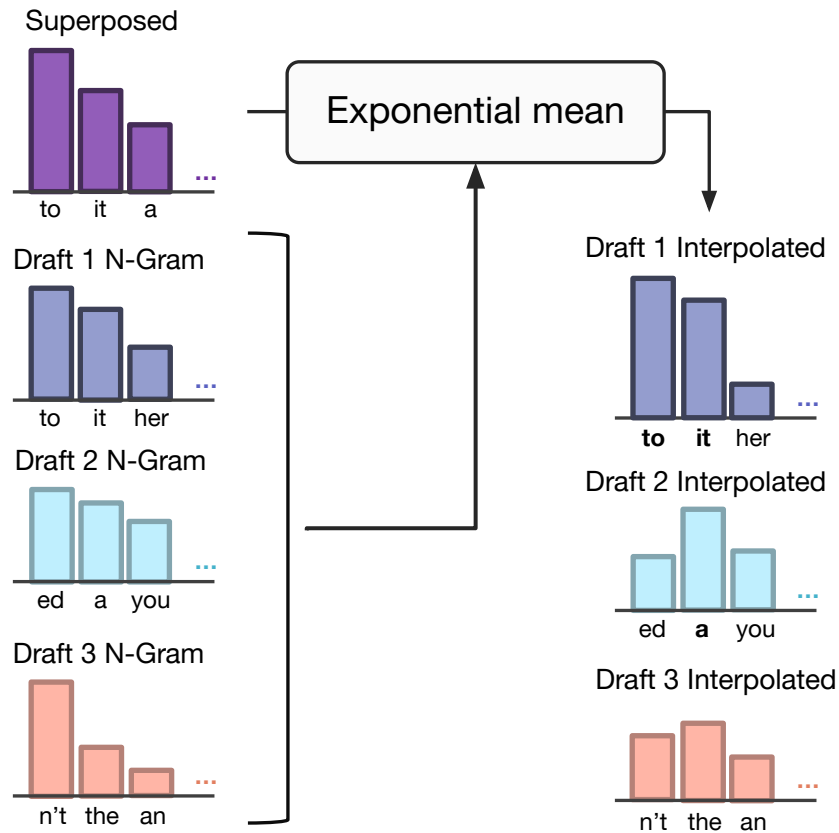


# Step 3: Interpolation

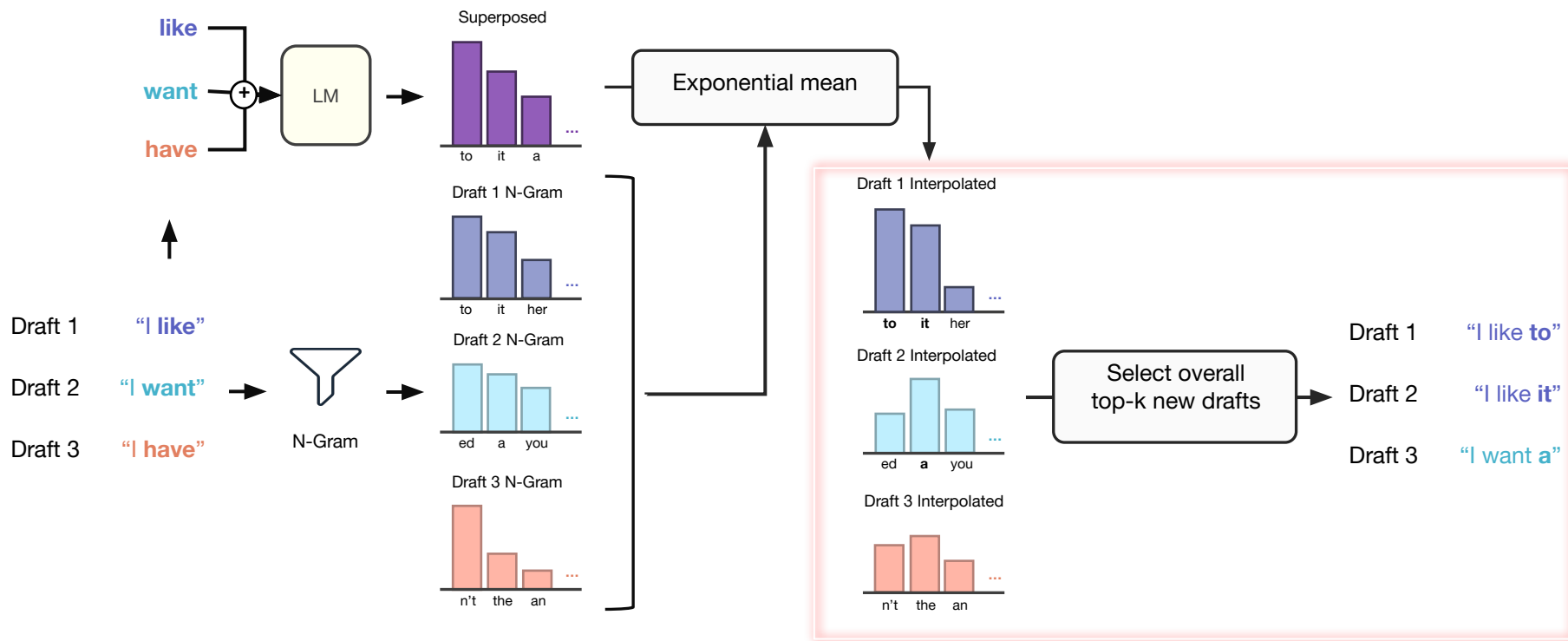


# Step 3: Interpolation

- Interpolate the N-Gram distributions with the LM distribution
- Draft-specific distributions



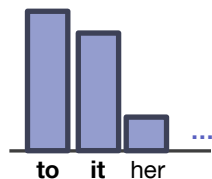
# Step 4: Update Drafts



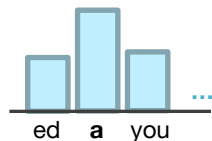
# Step 4: Update Drafts

1. Next tokens form  $k^2$  new draft options
  2. Rank using joint probability of tokens and drafts
  3. Update draft store
- Repeat!!!**

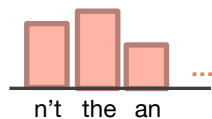
Draft 1 Interpolated



Draft 2 Interpolated



Draft 3 Interpolated



Select overall  
top-k new drafts

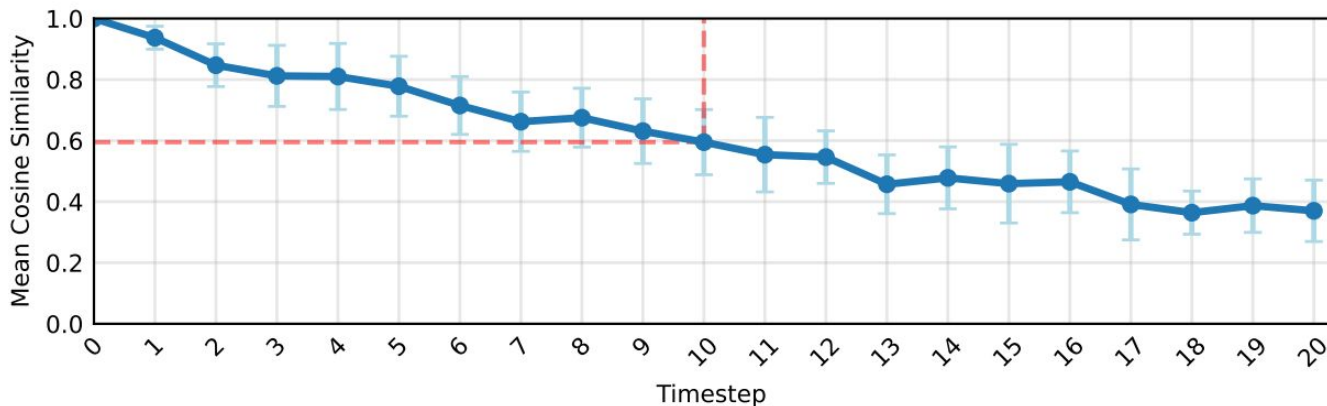
Draft 1 “I like to”

Draft 2 “I like it”

Draft 3 “I want a”

# Why does Superposed Decoding work?

- Layer embeddings using Superposed Decoding linearly relate to those of Beam Search drafts
  - 10 randomly sampled batches of 10 prefixes each (100 total prefixes)
- High linearity up to 10 timesteps - optimal generation length



# Example #1

	Text
OpenWebText Prefix	When I worked as a scout for the Carolina Panthers in the
Nucleus Sampling	1990s, I would often
Superposed Decoding	1990s, I was <b>always</b> 1990s, I was <b>a</b> 1990s, I was <b>responsible</b>

## Example #2

	Text
OpenWebText Prefix	Over a century ago, the RMS Titanic's fate
Nucleus Sampling	was sealed when it struck an iceberg on
Superposed Decoding	was sealed when it <b>struck</b> an iceberg <b>and</b> was sealed when it <b>hit</b> an iceberg <b>and</b> was sealed when it <b>hit</b> an iceberg <b>on</b>



# III. Results

# Experimental Setup

- Implement on Llama-2-7B
- N-Gram Models constructed using 200M tokens from RedPajama



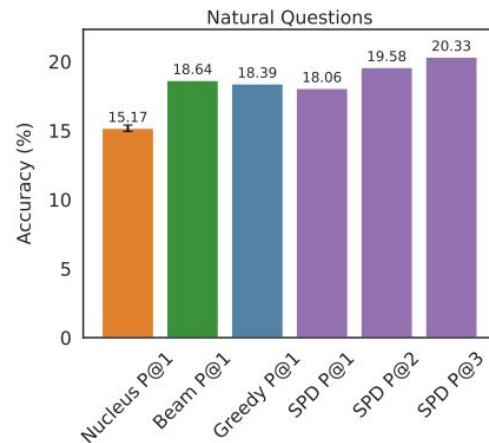
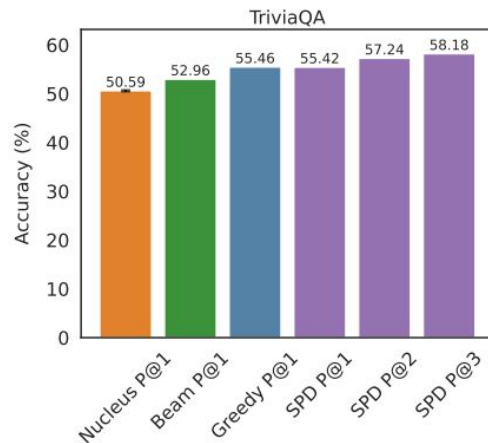
# Coherency

- Test on OpenWebText (10 tokens generated)
- Expect at least one SPD draft to be equal to Nucleus  
Sampling & others come free

	Nucleus	Beam/Greedy	N-Gram	Superposed Decoding			
Draft #	-	-	-	1	2	3	Best
Avg Perplexity	5.17	3.77	152.75	5.03	7.97	10.05	4.63

# Accuracy

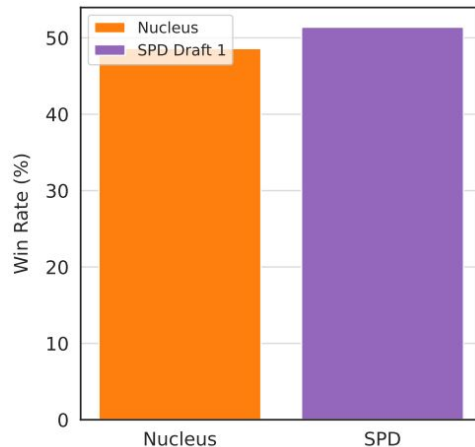
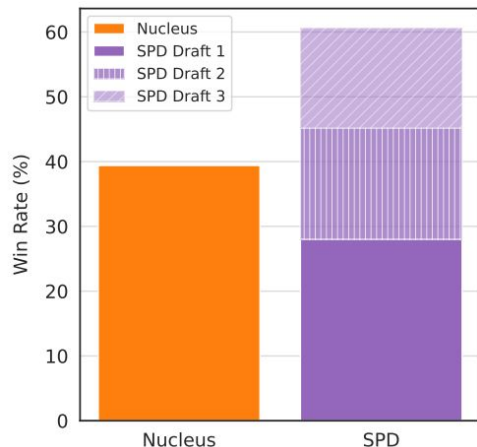
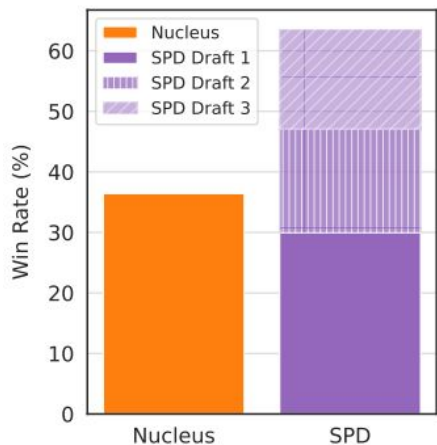
- Tested on TriviaQA and Natural Questions
- SPD gives more drafts @ same compute
- Extra drafts increase likelihood of factually accurate generations



# Human Evaluation

Three Surveys:

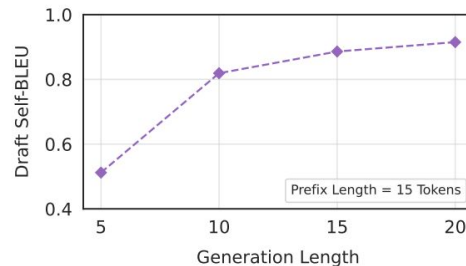
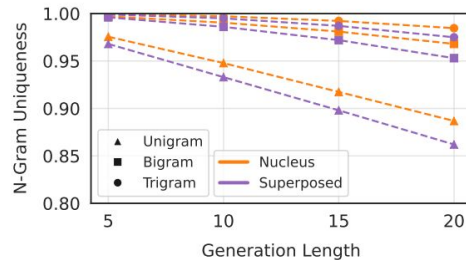
1. Constant Compute: 3 SPD vs 1 Nucleus (707 prefixes)
2. Unequal Compute: 3 SPD vs 2 Nucleus (100 prefixes)
3. Equal Number: 1 SPD vs 1 Nucleus (100 prefixes)



# Ablations

## Superposed Decoding:

- Does not suffer degeneration
- Increases diversity with smaller generation length
- Flawlessly extends to Mistral 7B



	Nucleus	Superposed Decoding			
Draft #	-	1	2	3	Best
Avg Perplexity	11.42	11.34	12.74	13.63	10.87

# Complementary Benefits

- Superposed Decoding's benefits are *completely complementary* to other decoding methods
- SPD offers local search at *no extra cost*
  - Freely expands global search (Nucleus Sampling) or other local search (Beam Search)

Prefix	Nucleus Sampling (k = 3)	3 x Superposed Decoding
Melbourne is	Melbourne is a great city, with Melbourne is a city of many different Melbourne is the capital city of Victoria	Melbourne is a great city, with a lot of things Melbourne is a great city, with a lot to things Melbourne is a great city, with a lot of history Melbourne is a city of many different cultures and relig Melbourne is a city of many different cultures, relig Melbourne is a city of many different cultures and languages Melbourne is the capital city of Victoria, Australia. It Melbourne is the capital city of Victoria and Australia. It Melbourne is the capital city of Victoria, Australia. The

# Test-Time Compute Scaling

- Repeated sampling (Brown et al., 2024) -> increased samples improve performance
- Extend Nucleus Sampling drafts with 2 or 3 SPD drafts free of cost

## TriviaQA

Compute (k)	1	10	20	30	40	50	60	70	80	90	100
NS	51.04	68.75	70.31	71.87	72.92	74.48	74.74	75.26	75.78	76.30	76.56
NS + 2 SPD	51.30	68.75	70.57	72.66	74.74	75.78	76.30	76.82	78.39	79.17	79.43
NS + 3 SPD	<b>51.82</b>	<b>70.57</b>	<b>74.22</b>	<b>75.52</b>	<b>77.34</b>	<b>77.87</b>	<b>78.39</b>	<b>78.65</b>	<b>79.17</b>	<b>79.43</b>	<b>79.95</b>

## Natural Questions

Compute (k)	1	10	20	30	40	50	60	70	80	90	100
NS	14.32	<b>32.55</b>	<b>36.98</b>	38.54	40.36	41.15	41.67	41.93	42.19	42.71	42.97
NS + 2 SPD	15.36	31.25	34.90	38.02	39.84	41.41	41.67	42.45	43.75	43.75	43.75
NS + 3 SPD	<b>15.63</b>	31.25	<b>36.98</b>	<b>39.06</b>	<b>41.15</b>	<b>42.71</b>	<b>43.75</b>	<b>43.75</b>	<b>44.27</b>	<b>44.79</b>	<b>45.57</b>



# Takeaways

## Benefits:

- Coherent and human preferred
- Factual
- Increase effective batch size
- Inference compute scaling

## Applications:

- Tabnine
- Microsoft Copilot
- ...and more!!!

