

Persistence Homology Distillation for Semi-supervised Continual learning

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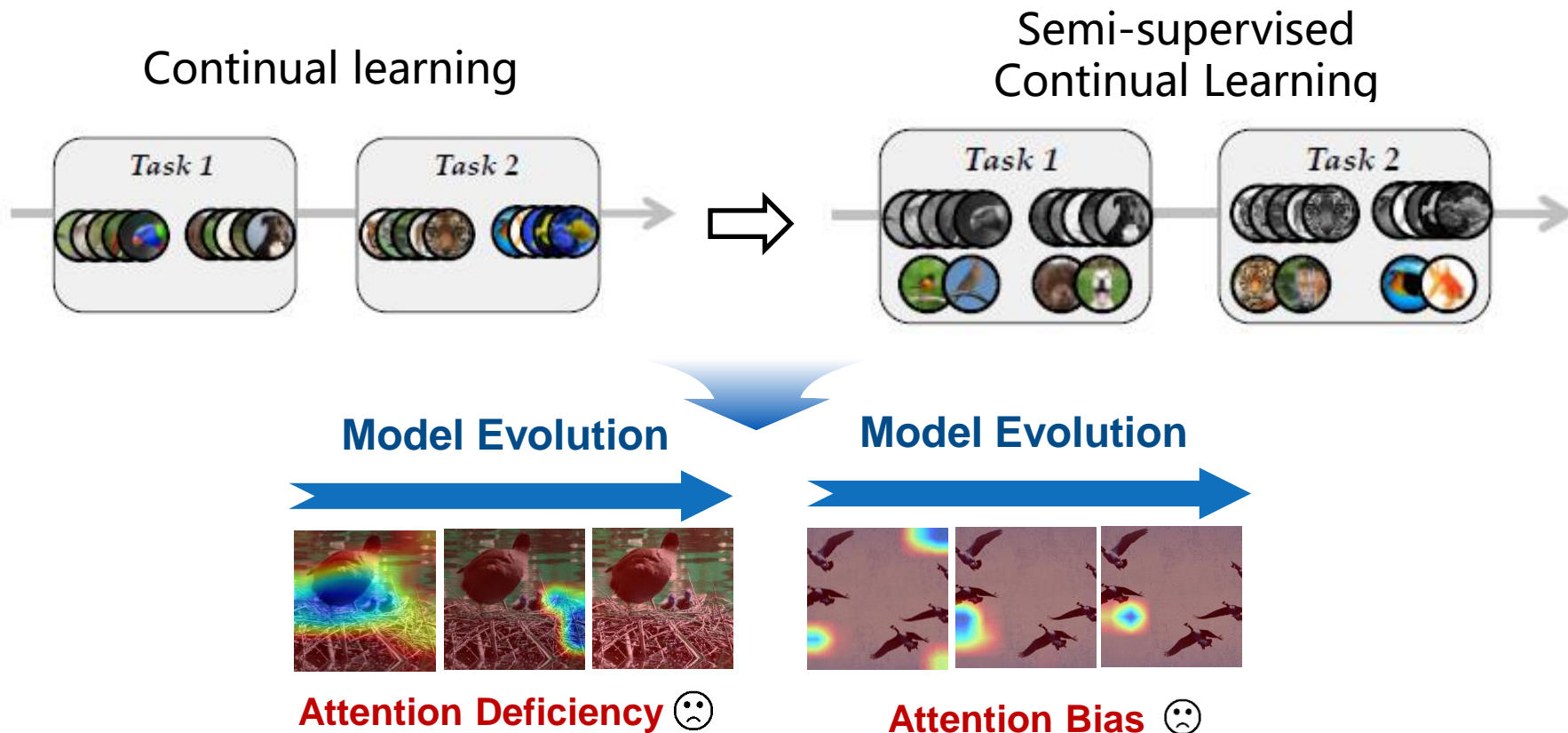
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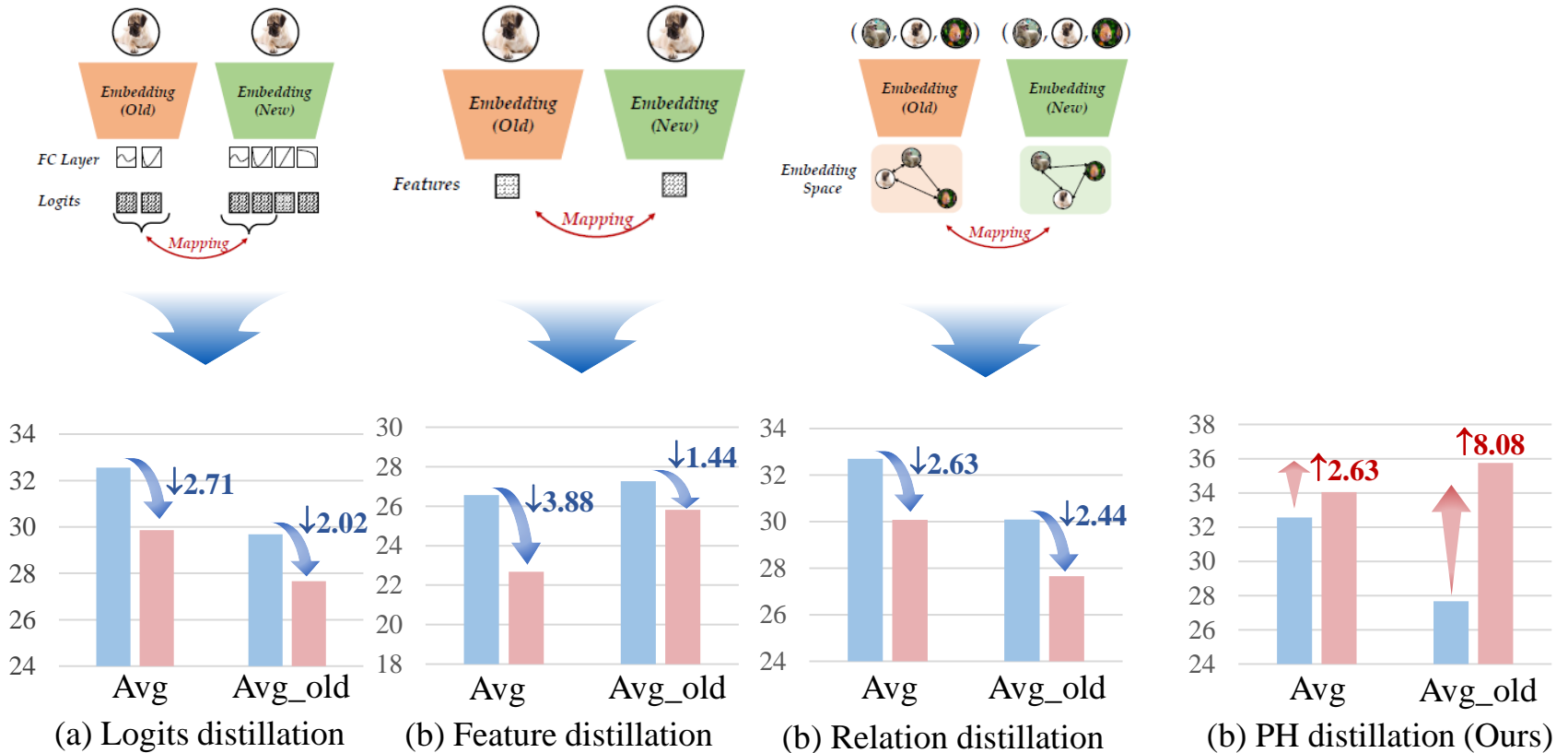
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Background



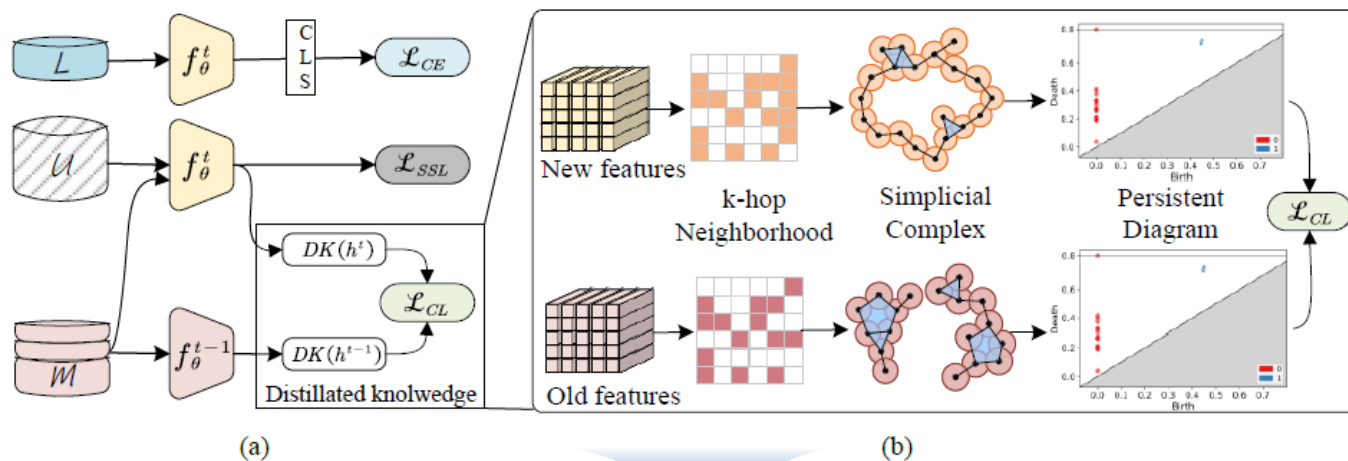
Knowledge Distillation



Fan Y, Wang Y, Zhu P, Chen D, Hu Q. [Persistence Homology Distillation for Semi-supervised Continual Learning](#). NIPS, 2024.

A more powerful noise insensitive distillation is needed for SSCL

Main contribution: persistence homology distillation



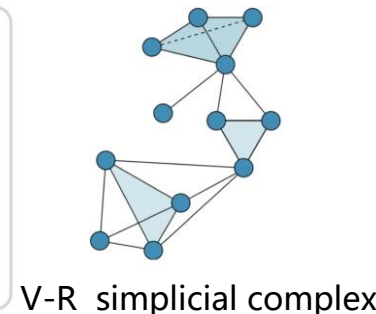
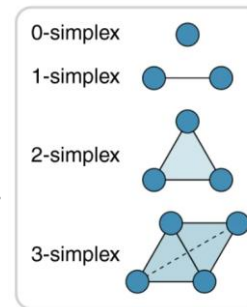
- We utilize simplicial complexes to approximate vision data and explore **stable topological feature representation** of unlabeled data in semi-supervised continual learning.
- • We propose a novel **persistence homology distillation strategy** for SSCL that is insensitive to noise information interference, and devise **an accelerating algorithm** to reduce computation costs.
- • We demonstrate that our method outperforms existing methods on several benchmarks, and highlights the potential of utilizing unlabeled data to overcome catastrophic forgetting.

Persistence Homology Distillation for Semi-supervised Continual learning

■ Preliminary of Persistence Homology

■ **Simplicial complex** : built from a set of simplices that satisfies Closure under Faces and Intersection Property.

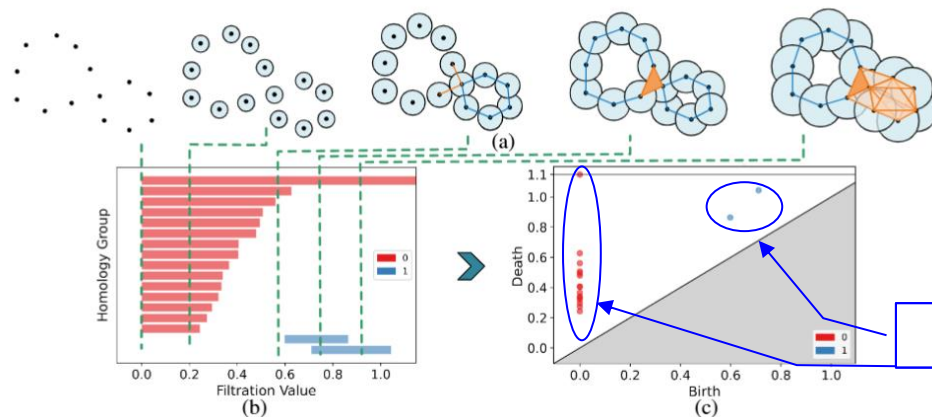
■ **k-simplex**: k-dimensional polytope



■ **Persistence homology**: quantifying topological features over a range of length scales by defining a filtration on it.

$$\text{Filtration: } K_r = \delta_X^{-1}((-\infty, r]) = \{y \in \mathbb{R}^d | \delta_X(y) \leq r\} = \cup_{x \in X} B(x, r)$$

$$\emptyset = K_0 \subset K_1 \subset \dots \subset K_m = K,$$



(x_σ, y_σ) : one simplex σ born in x_σ and dies in y_σ

$$Dgm = \{(x_\sigma, y_\sigma) \in \mathbb{R}^2 : x_\sigma < y_\sigma\} \cup \Delta$$

Value: Breaking the limitations of binary topological relationships

■ Persistence Homology Distillation

■ Topological representation:

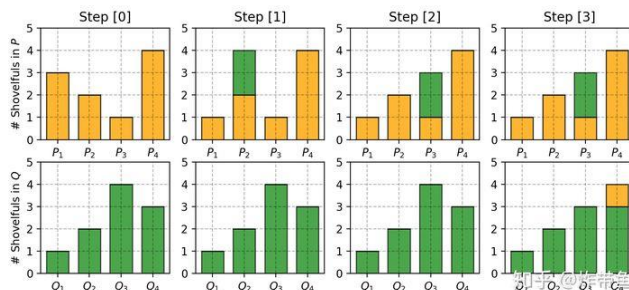
■ Adjacency Matrix: $G(V, E)$ $W_{ij} = \begin{cases} 1, & \text{if } s_{ij} \geq \beta \\ 0, & \text{if } s_{ij} < \beta \end{cases}$ $s_{ij} = \langle h_i, h_j \rangle = \frac{h_i h_j}{\|h_i\| \|h_j\|}$

■ k-hop neighborhood : $\mathcal{N}(x_i, k)$ $x_j \in \mathcal{N}(x_i, k)$ if the shortest path between x_i and x_j is k.

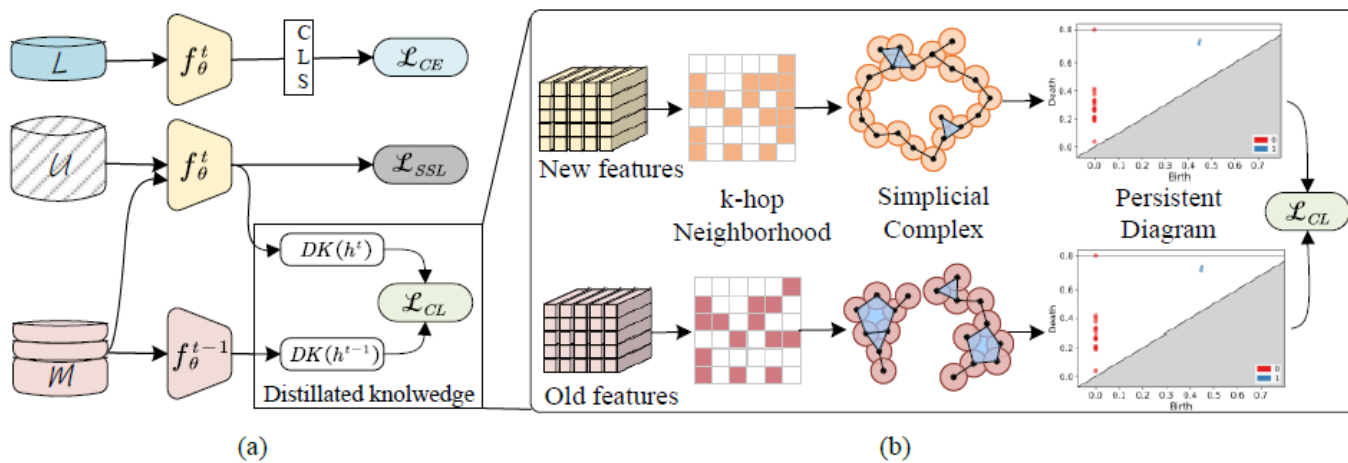
■ h-dim local persistence diagram: $Dgm_h(\mathcal{N}(x_i, k))$

■ Topological distance : p-Wasserstein distance (Optimal transport distance)

$$d_{\mathcal{N}_x^k}(f_{old}, f_{new}) = \inf_{\gamma} \left(\sum_{u \in Dgm_h(\mathcal{N}_x^k, f_{old}) \cup \Delta} \|u - \gamma(u)\|^p \right)^{\frac{1}{p}}$$



■ Persistence Homology Distillation



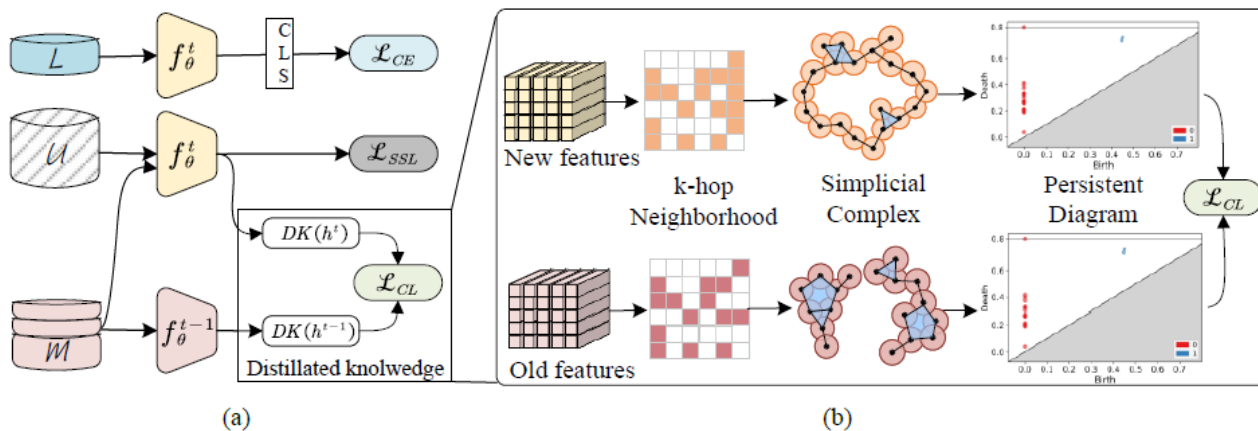
Overall Loss:

$$\mathcal{L}_{sscl} = \mathcal{L}_{CE} + \mathcal{L}_{SSL} + \lambda \mathcal{L}_{CL}$$

Persistence Homology
Distillation loss:

$$\mathcal{L}_{hd} = \frac{1}{|S|} \sum_{x \in S} d_{N_x^k}(f_{old}, f_{new})$$

■ Stability Analysis



Theorem 1. Given the two feature space of point data as \mathcal{P}_0 and \mathcal{P}_1 , for all $p \geq 1$ and $h \in \mathbb{Z}^+$, we have

$$W_p(Dgm_h(\mathcal{R}(\mathcal{P}_0)), Dgm_h(\mathcal{R}(\mathcal{P}_1))) \leq \binom{M-1}{k}^{\frac{1}{p}} W_p^{pair}(\mathcal{P}_0, \mathcal{P}_1), \quad (7)$$

where $Dgm_h(\mathcal{R}(\mathcal{P}_0))$ and $Dgm_h(\mathcal{R}(\mathcal{P}_1))$ are the h -dimensional persistence diagram for the Vietoris-Rips filtration on the point set \mathcal{P}_0 and \mathcal{P}_1 respectively. W_p^{pair} represents the pair-wise distance between the point set $W_p^{pair}(\mathcal{P}_0, \mathcal{P}_1) = \inf_{\phi} (\sum_{u,v \in \mathcal{P}_0} |\|v-u\| - \|\phi(v) - \phi(u)\||^p)^{\frac{1}{p}}$, where ϕ is a bijection between the two set \mathcal{P}_0 and \mathcal{P}_1 .

■ Experiment Results

- Better adaptable to unlabeled data compared to other knowledge distillation methods

Table 3: Comparison of different knowledge distillation methods applied on SSCL.

Method	Type	CIFAR10		CIFAR100	
		5%	25%	5%	25%
iCaRL[34]	logits	79.2	78.8	31.3	41.4
Foster[40]	logits	75.0	70.4	24.6	38.8
LUCIR[20]	feature	75.2	74.7	32.0	32.6
Podnet[12]	feature	57.9	69.0	21.4	21.1
R-DFIL[16]	relation	78.5	78.8	34.7	34.2
DSGD[14]	relation	79.1	79.0	35.9	43.1
TopKD[22]	topology	78.7	79.8	35.4	41.9
PsHD	topology	81.5	81.4	38.8	43.2

- Stability to noise interference

Table 4: Comparison of distillation methods with Gaussian noise interference. σ is the standard deviation.

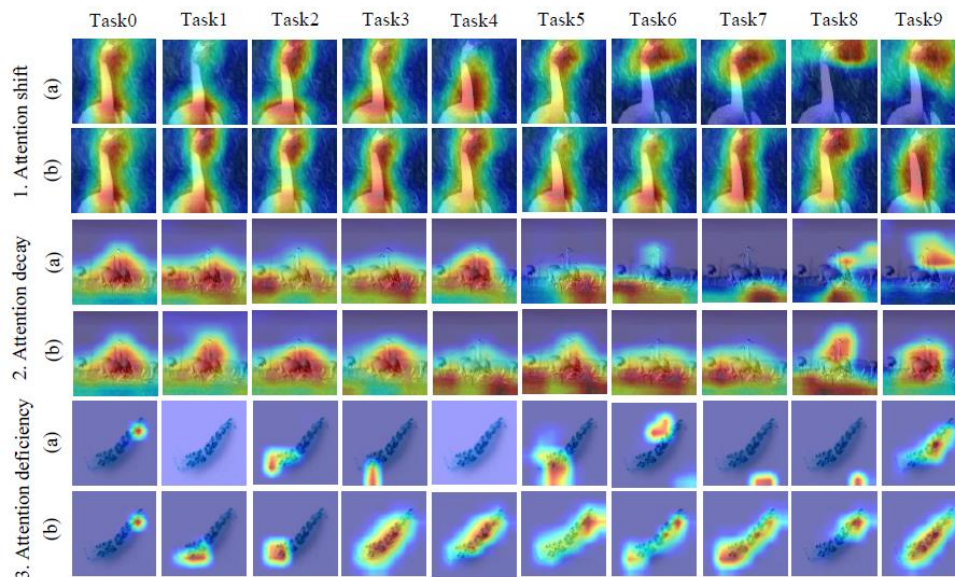
σ	Podnet[12]		LUCIR[20]		R-DFCIL[16]		DSGD[14]		TopKD[22]		PsHD	
	BWT↓	ACC↑	BWT↓	ACC↑	BWT↓	ACC↑	BWT↓	ACC↑	BWT↓	ACC↑	BWT↓	ACC↑
0.2	31.8	55.6	21.8	71.5	19.2	77.5	18.1	76.7	19.7	76.5	14.0	78.7
1.0	44.4	27.9	34.3	57.3	28.2	62.1	27.1	64.2	23.0	67.2	17.7	70.9
1.2	49.8	34.6	36.4	56.4	26.4	61.8	23.7	64.1	22.8	65.8	18.3	67.8

■ Experiment Results

■ Ablation Study

Table 5: Ablation study of proposed persistence homology distillation

Method	\mathcal{L}_{SSL}	\mathcal{L}_{hd}	CIFAR10_5%		CIFAR10_25%		CIFAR100_5%		CIFAR100_25%	
			avg	last	avg	last	avg	last	avg	last
iCaRL	✓		83.7	79.2	82.9	78.8	54.2	36.1	58.4	41.1
	✓	✓	85.3 _{+1.5}	80.8 _{+1.6}	85.4 _{+2.6}	80.5 _{+1.7}	56.4 _{+2.2}	38.8 _{+2.7}	59.2 _{+0.8}	42.2 _{+1.1}
DER	✓		86.1	81.2	84.9	81.4	57.8	46.3	68.1	57.2
	✓	✓	86.2 _{+0.1}	81.8 _{+0.6}	87.9 _{+3.0}	83.4 _{+2.0}	58.2 _{+0.4}	47.2 _{+0.9}	68.3 _{+0.2}	57.7 _{+0.5}



Thanks for your listening

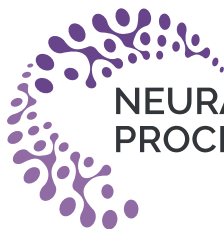
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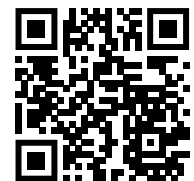
NEURAL INFORMATION
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Paper



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