

Policy Learning Using Weak Supervision

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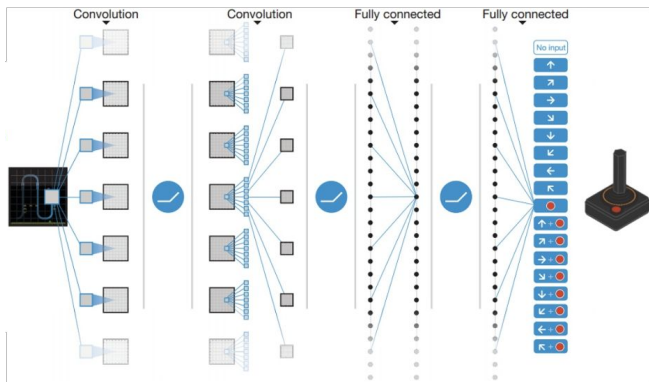


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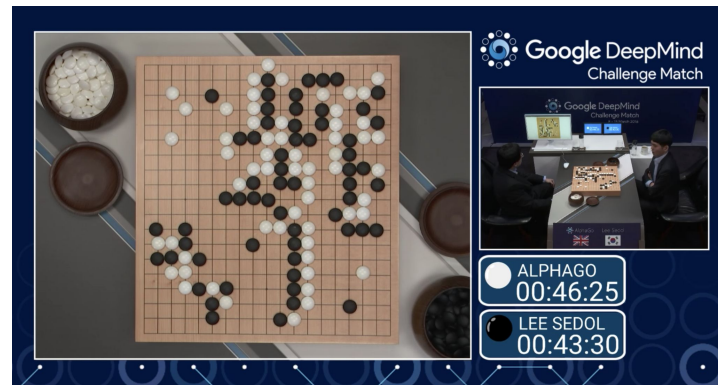


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Deep Learning in Sequential Decision Making



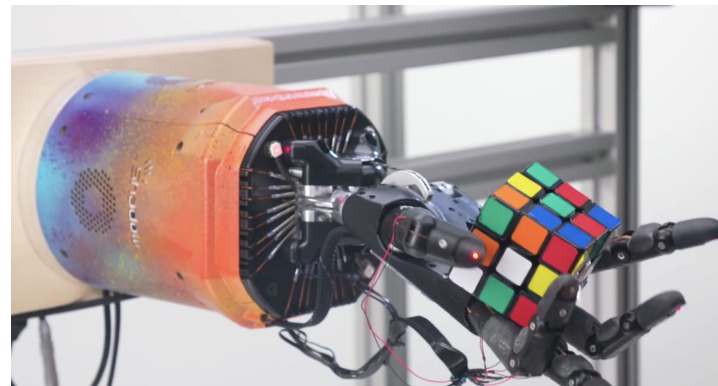
Atari2600 Games [Mnih et al., 2015]



AlphaGo [Silver et al., 2017]



Self-Driving [Amini et al., 2020]

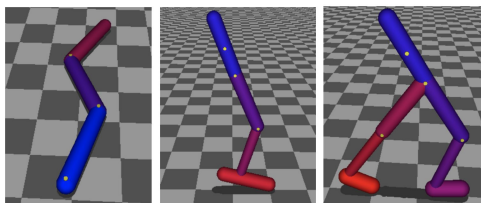


Self-Driving [OpenAI, 2019]

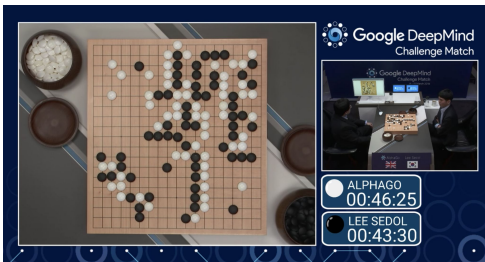
Markov Decision Process (MDP)



[Mnih et al., 2013]



[Schulman et al., 2015]

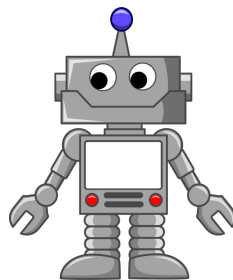


[AlphaGo versus Lee Sedol]



MDP: $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{R}, \mathcal{P}, \gamma \rangle$

Action $a_t \in \mathcal{A}$



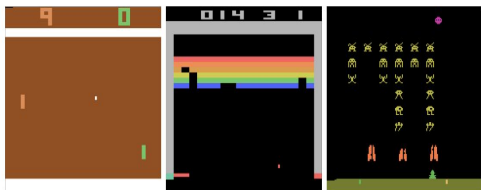
Agent

$\pi : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$

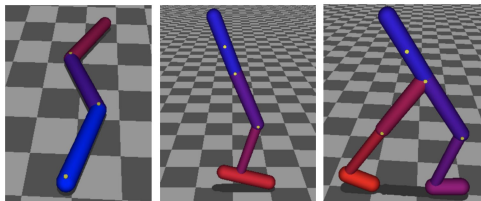


Environment

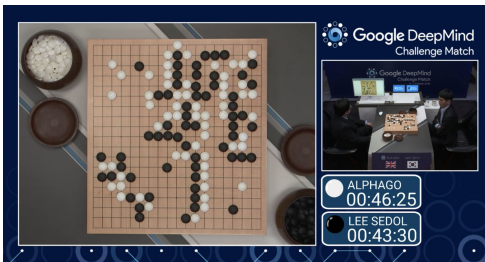
Markov Decision Process (MDP)



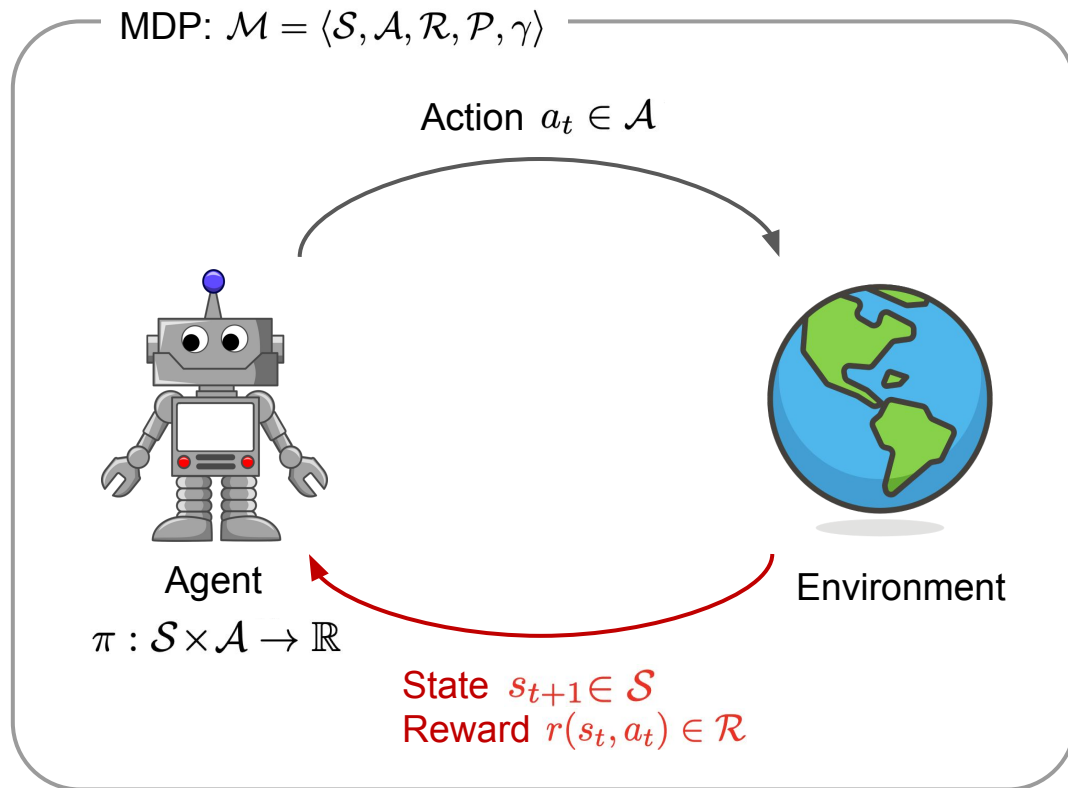
[Mnih et al., 2013]



[Schulman et al., 2015]



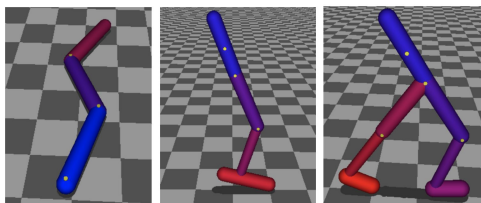
[AlphaGo versus Lee Sedol]



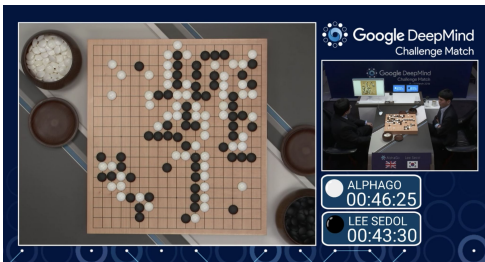
Markov Decision Process (MDP)



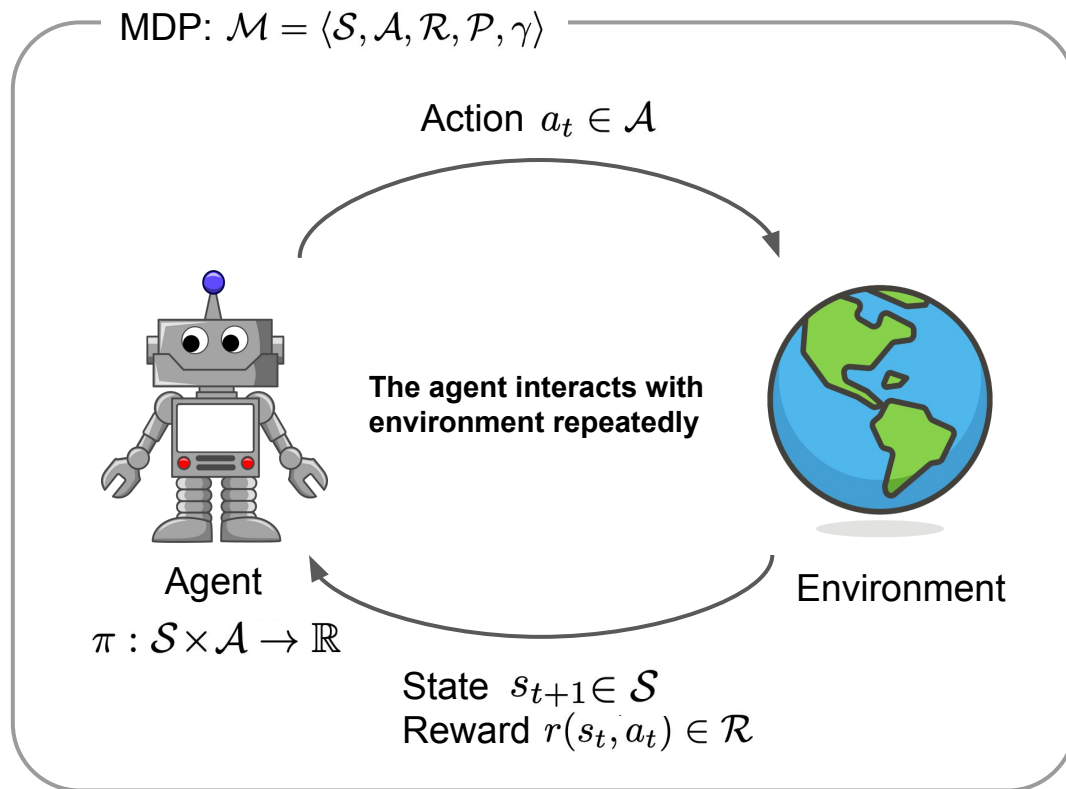
[Mnih et al., 2013]



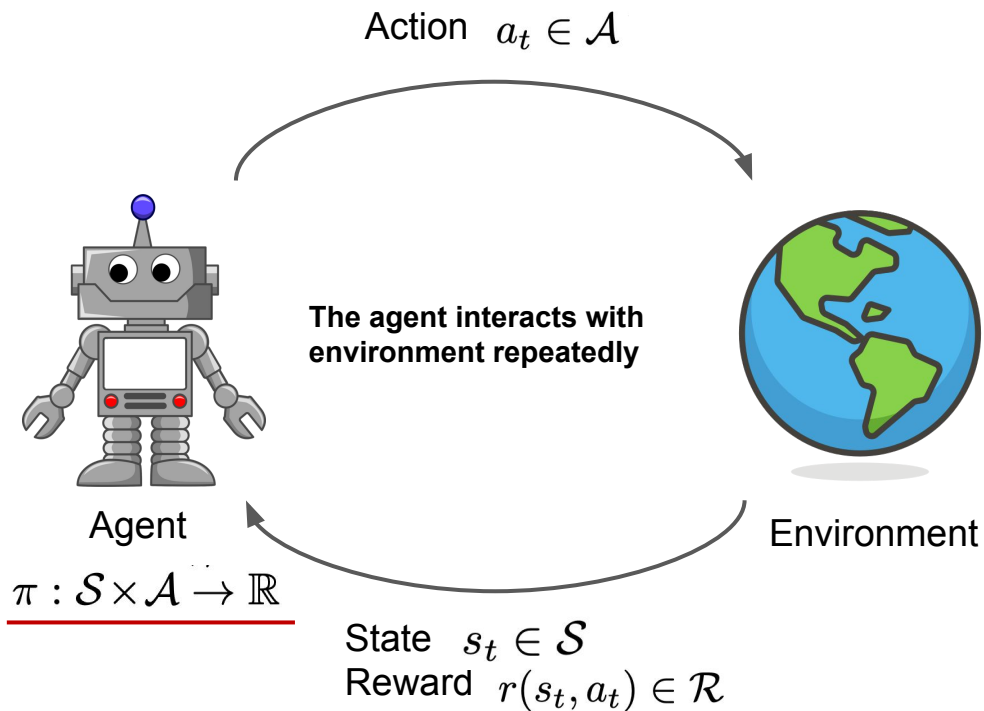
[Schulman et al., 2015]



[AlphaGo versus Lee Sedol]



Reinforcement Learning



Generated trajectory:

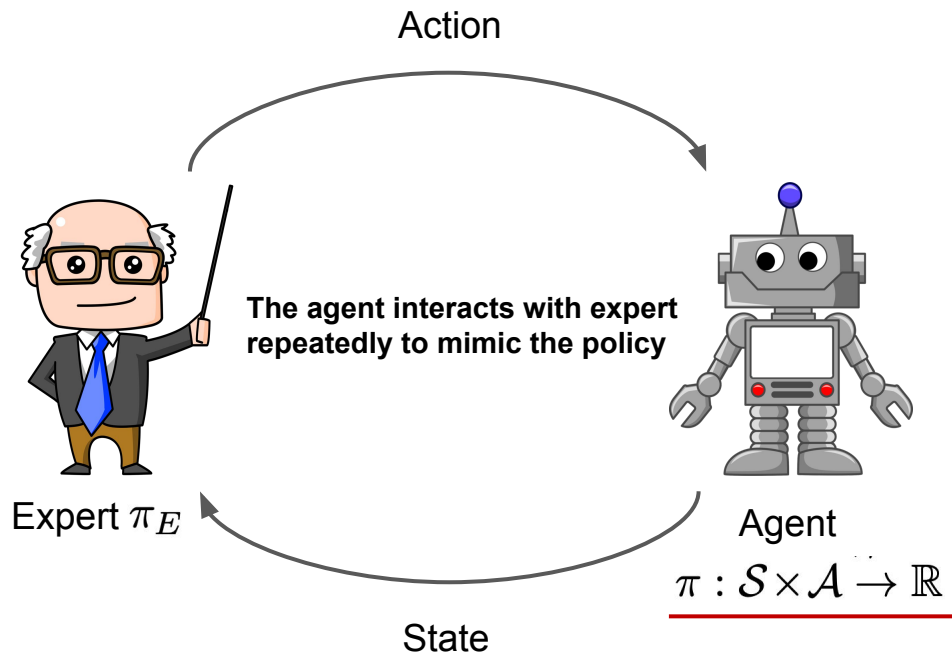
$$\tau = \{(s_t, a_t, r_t)\}_{t=0}^T$$

Objective: maximize the expected reward

$$J(\pi) = \mathbb{E}_{(s_t, a_t, r_t) \sim \tau} [\sum_{t=0}^T \gamma^t r_t]$$

Supervision signal: *reward*

Imitation Learning



Expert demonstrations

$$D_E = \{(s_i, a_i)\}_{i=1}^N$$

Behavioral Cloning Objective:
maximize the log-likelihood

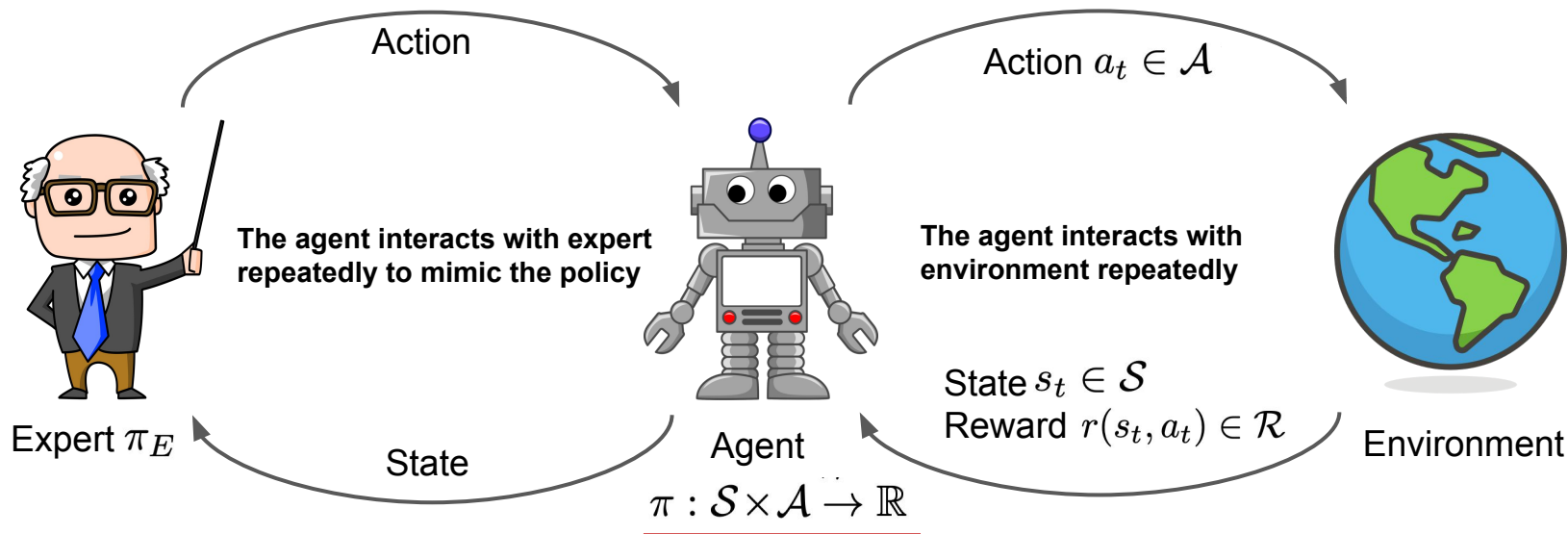
$$J(\pi) = \mathbb{E}_{(s,a) \sim D_E} [\log \pi(a|s)]$$

Supervision signal: *expert action*

Hybrid Learning (RL + IL)

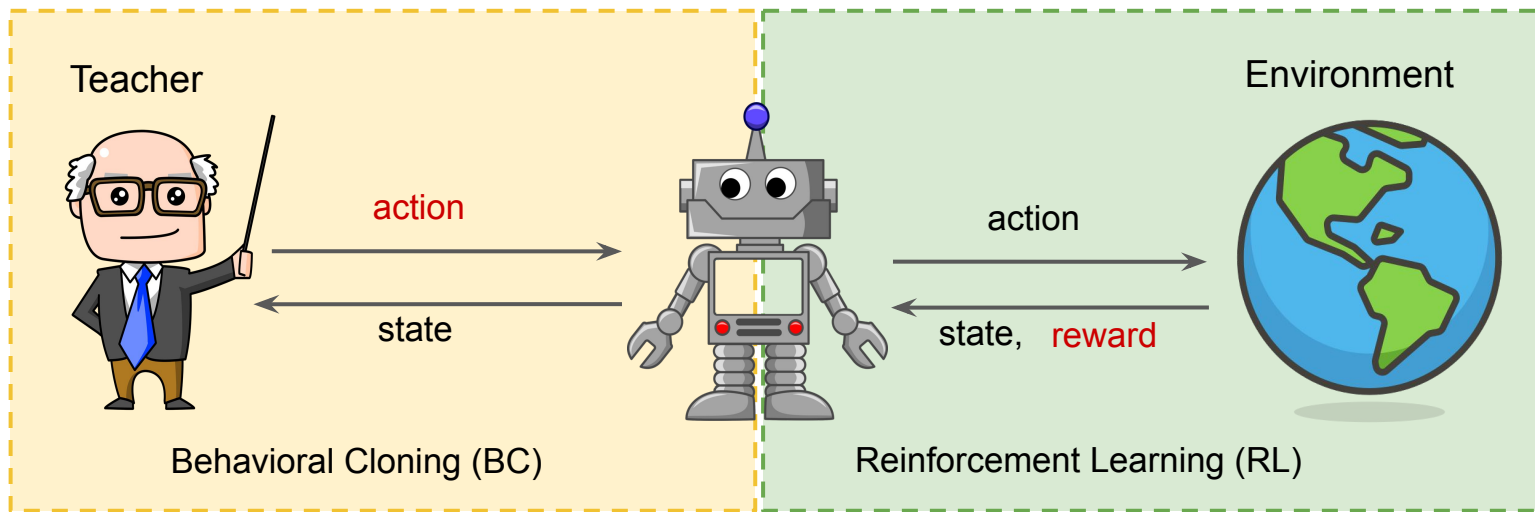
Supervision signal: *reward + expert action*

Hybrid objective: $J(\pi) = \lambda_1 \mathbb{E}_{(s_t, a_t, r_t) \sim \tau} \left[\sum_{t=0}^T \gamma^t r_t \right] + \lambda_2 \mathbb{E}_{(s, a) \sim \mathcal{D}_E} [\log \pi(a|s)]$



Policy Learning

Summary:



 BC

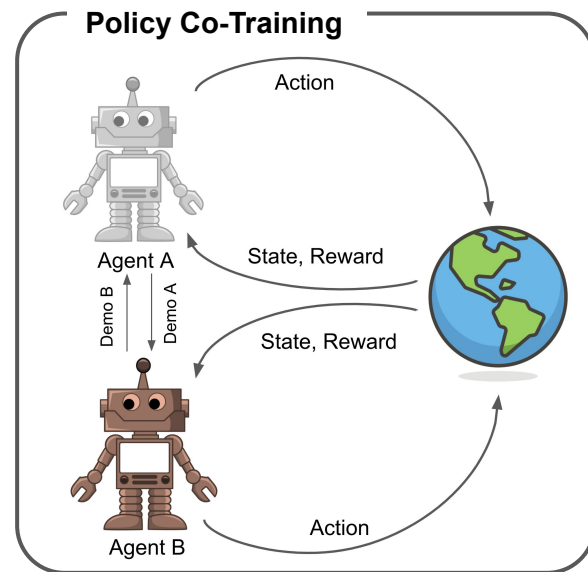
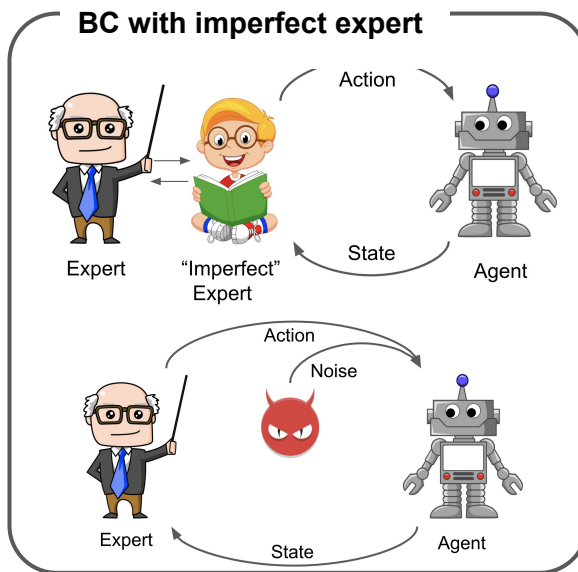
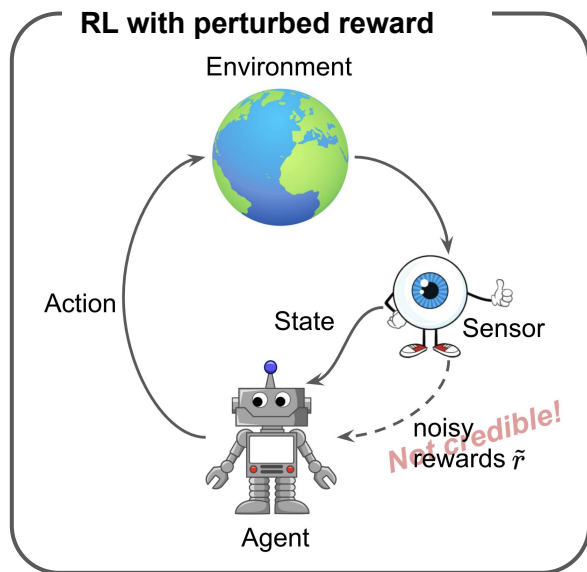
 RL

 +  Hybrid Learning

Weak supervision signals are everywhere!

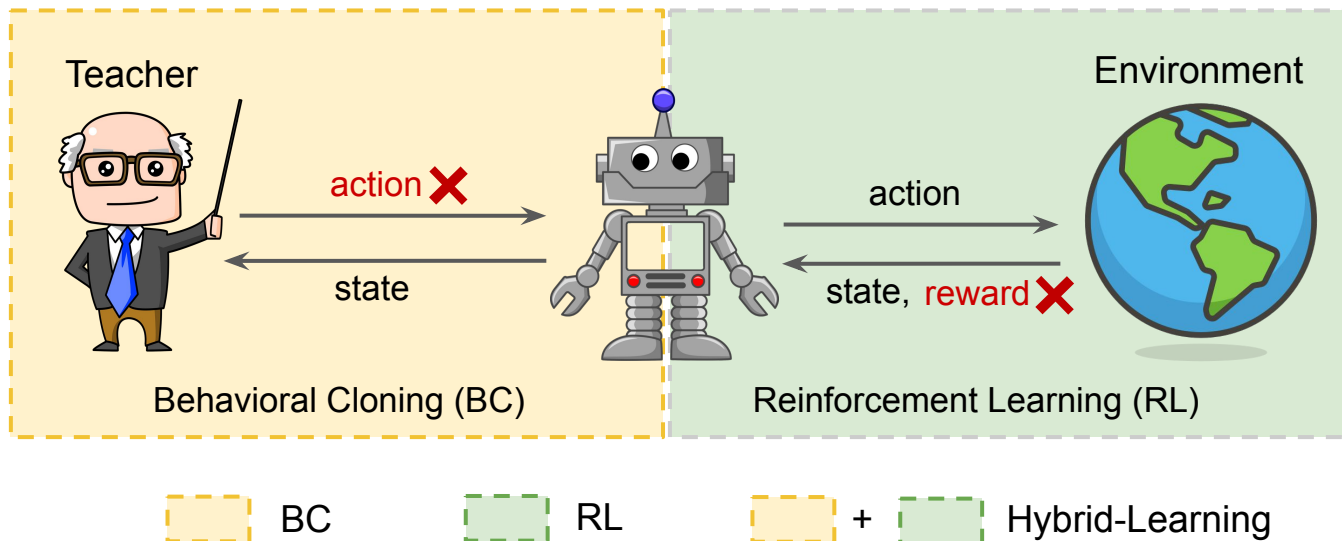
Weak Supervision:

- **RL:** The reward may be collected through sensors thus noisy
- **IL:** The demonstrations by an expert are often imperfect due to limited resources



Weakly Supervised Policy Learning

Problem: Supervision signals \tilde{Y} (either reward or expert's demonstrations) are *not credible!*

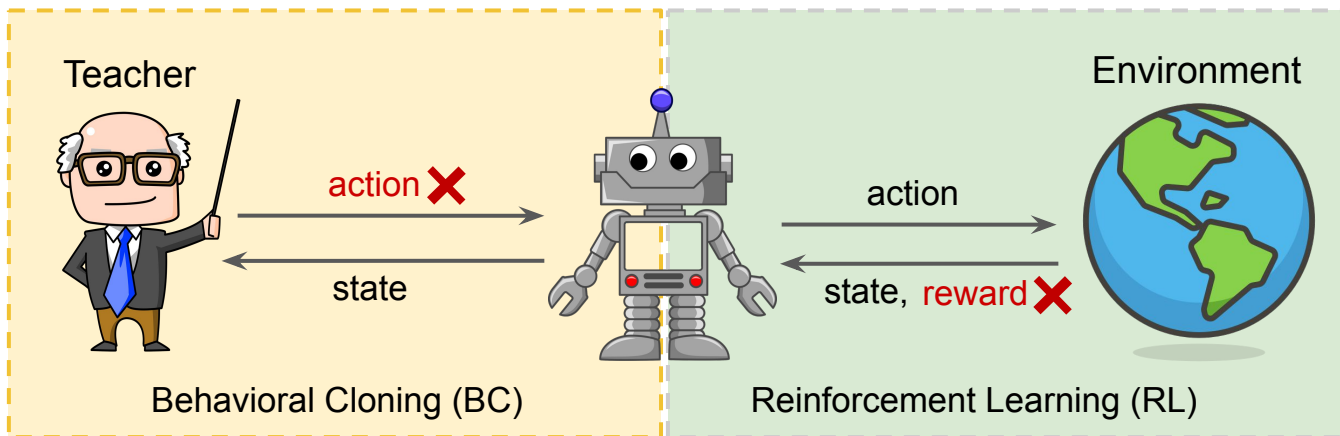


Weak Supervision:

- **RL:** The reward may be collected through sensors thus noisy
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Weakly Supervised Policy Learning

Weakly Supervised Policy Learning $\{(s_i, a_i), \tilde{Y}_i\}_{i=1}^N$

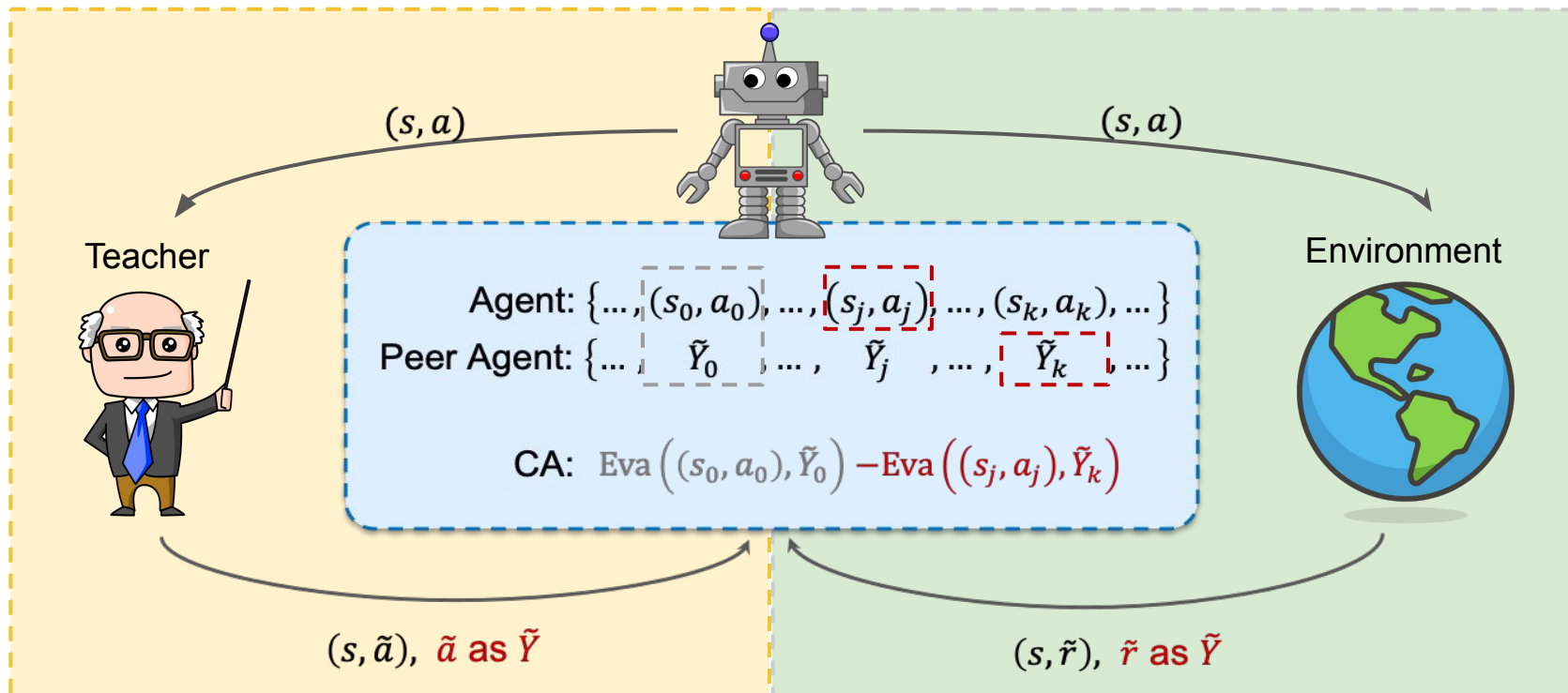


 BC  RL  +  Hybrid-Learning

- Objective: $J(\pi) = \mathbb{E}_{(s,a) \sim \tau} \left[\text{Eva}_{\pi} \left((s, a), \tilde{Y} \right) \right]$

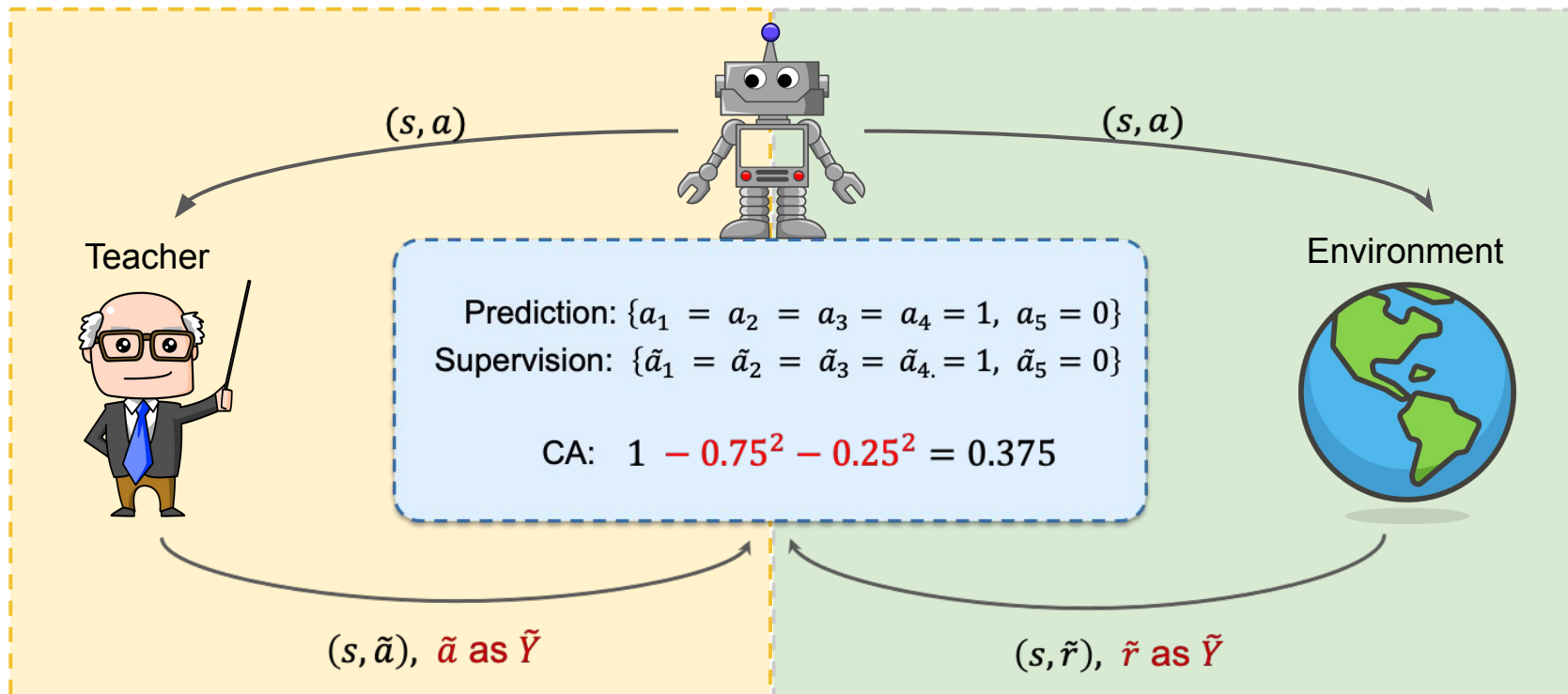
Correlated Agreement (CA)

Solution - CA with weak supervision: $\text{Eva}_\pi((s_i, a_i), \tilde{Y}_i) - \text{Eva}_\pi((s_j, a_j), \tilde{Y}_k)$



Correlated Agreement (CA)

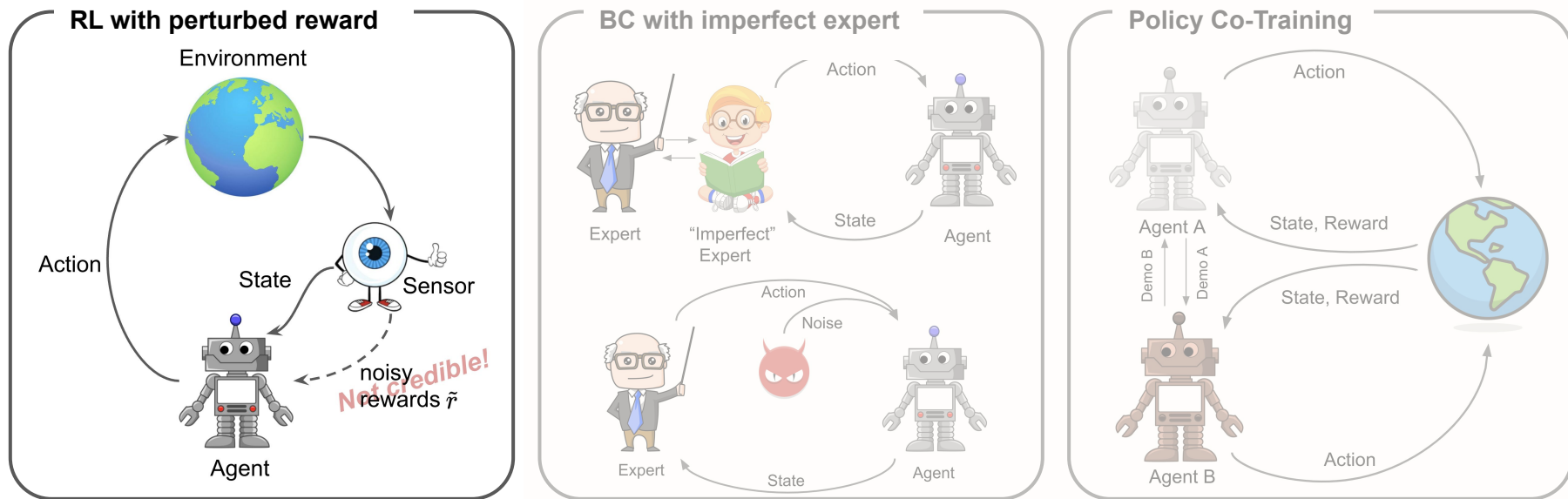
Solution - CA with weak supervision: $\text{Eva}_\pi((s_i, a_i), \tilde{Y}_i) - \text{Eva}_\pi((s_j, a_j), \tilde{Y}_k)$



PeerPL: A Unified Framework for Weakly Supervised PL

Solution - CA with weak supervision: $\text{Eva}_\pi((s_i, a_i), \tilde{Y}_i) - \text{Eva}_\pi((s_j, a_j), \tilde{Y}_k)$

PeerRL



We assume the noisy reward \tilde{r} is generated following a certain function $F : \mathcal{R} \rightarrow \tilde{\mathcal{R}}$.

- Discrete with $|\mathcal{R}|$ levels.
- Characterized via an **unknown** matrix $C_{|\mathcal{R}| \times |\mathcal{R}|}^{\text{RL}}$

$$r(s, a) \xrightarrow{C_{|\mathcal{R}| \times |\mathcal{R}|}^{\text{RL}}} \tilde{r}(s, a)$$

PeerRL handles the noisy reward by defining the peer RL reward:

$$\tilde{r}_{\text{peer}}(s, a) = \tilde{r}(s, a) - \xi \cdot \tilde{r}'$$

where $\tilde{r}' \stackrel{\pi_{\text{sample}}}{\sim} \{\tilde{r}(s, a) | s \in \mathcal{S}, a \in \mathcal{A}\}$ is a reward sampled over all state-action pairs according to a fixed policy π_{sample} .

$$\tilde{r}(s, a) \xrightarrow{\text{CA}} \tilde{r}_{\text{peer}}(s, a)$$

Our theory shows that peer RL rewards are robust to noisy rewards (see **Lemma 1 and Theorem 1**).

Why Peer Reward Works?

- **Hypothesis 1:** PeerRL reduces the bias (while with larger variance like Wang et al., 2020)

noisy reward:
$$\mathbb{E}[\tilde{r}] = \eta \cdot \left(\mathbb{E}[r] + \frac{e_+}{1 - e_- - e_+} r_- + \frac{e_-}{1 - e_- - e_+} r_+ \right)$$

peer reward:
$$\mathbb{E}[\tilde{r}_{\text{peer}}] = \eta \cdot (\mathbb{E}[r] - (1 - p_{\text{peer}})r_- - p_{\text{peer}}r_+)$$

potentially much larger than $(1 - p_{\text{peer}})$ and p_{peer} in high noise regime!

- **Hypothesis 2:** PeerRL helps break ties
 - “tie” states indicate that the rewards for different states are the same - unstable and uncertain
 - randomness in discretization model thus breaking ties - more informative for optimization

2-state Markov process (no actions)



$$r_1 \sim \text{clamp}[\mathcal{N}(0.6, 1), \min = 0, \max = 1]$$

$$r_2 \sim \text{clamp}[\mathcal{N}(0.4, 1), \min = 0, \max = 1]$$

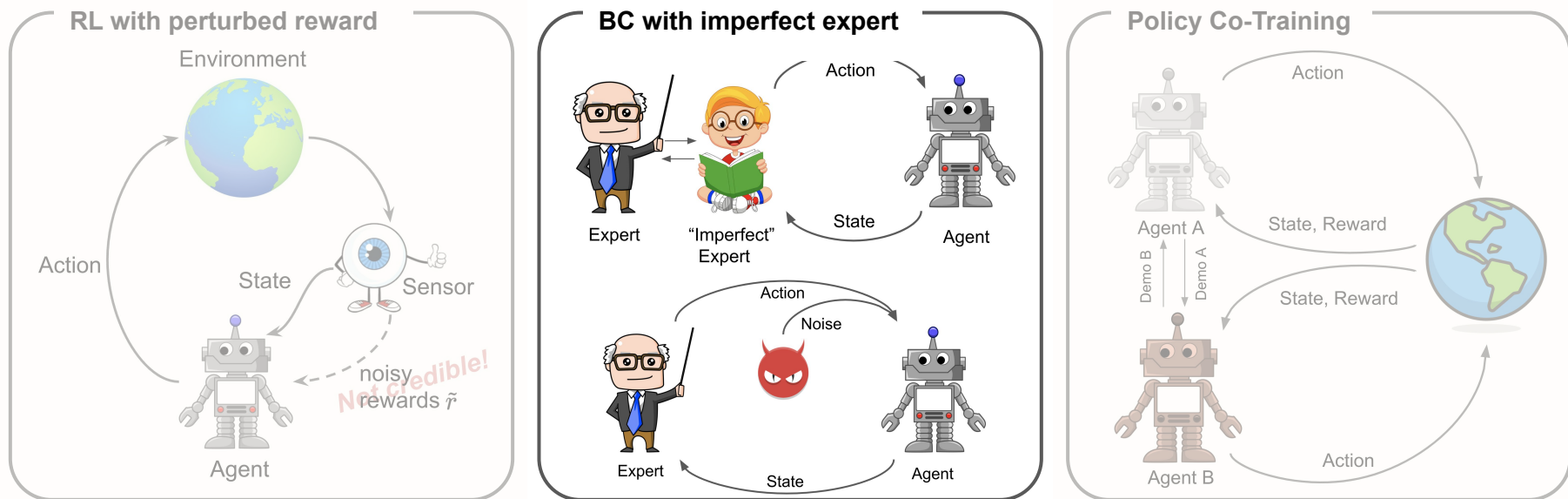
	Correct	Tie	Incorrect
Baseline	54.6%	5.6%	39.8%
PeerRL	58.0%	0.3%	41.7%

Tie breaking!

PeerPL: A Unified Framework for Weakly Supervised PL

Solution - CA with weak supervision:
$$\text{Eva}_{\pi}((s_i, a_i), \tilde{Y}_i) - \text{Eva}_{\pi}((s_j, a_j), \tilde{Y}_k)$$

PeerBC



Available weak demonstrations $\{(s_i, \tilde{a}_i)\}_{i=1}^N$ where $\tilde{a}_i \sim \tilde{\pi}_E(\cdot|s_i)$

- The noisy action \tilde{a}_i is independent of the state given the deterministic expert action $\pi_E(s)$
- The noise is characterized by an **unknown** confusion matrix

$$C_{|\mathcal{A}| \times |\mathcal{A}|}^{\text{BC}}$$

$$a_i \xrightarrow{C_{|\mathcal{A}| \times |\mathcal{A}|}^{\text{BC}}} \tilde{a}_i$$

Again, we use CA with weak supervision to handle the noise

- Taking cross-entropy loss for example

$$\text{Eva}_{\pi}^{\text{BC}}((s_i, a_i), \tilde{a}_i) \xrightarrow{\text{CA}} J^{\text{BC}}(\pi_{\theta})$$

-

$$J^{\text{BC}}(\pi_{\theta}) = \mathbb{E} \left[\text{Eva}_{\pi}^{\text{BC}}((s_i, a_i), \tilde{a}_i) \right] - \xi \cdot \mathbb{E} \left[\text{Eva}_{\pi}^{\text{BC}}((s_j, a_j), \tilde{a}_k) \right]$$

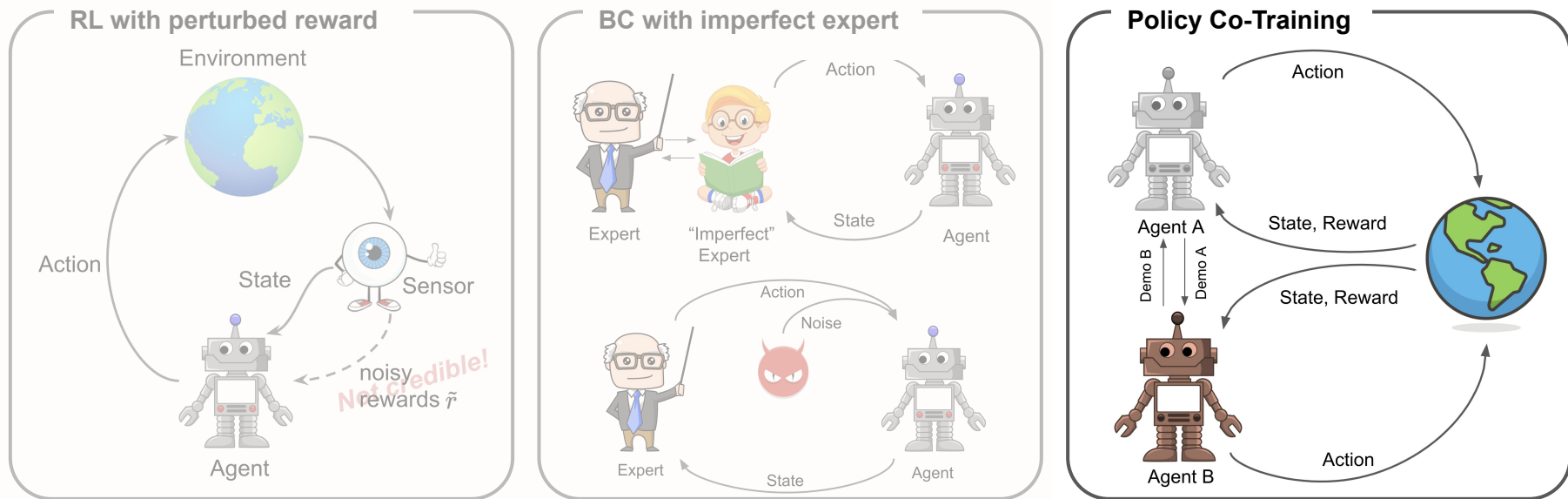
- where $\text{Eva}_{\pi}^{\text{BC}}(s, a, \tilde{a}) = -\ell(\pi_{\theta}, (s, \tilde{a})) = \log \pi_{\theta}(\tilde{a}|s)$.
- ... requires access to the expert policy, which requires a sufficient amount of weak demonstrations

(see Theorem 2)

PeerPL: A Unified Framework for Weakly Supervised PL

Solution - CA with weak supervision: $\text{Eva}_\pi((s_i, a_i), \tilde{Y}_i) - \text{Eva}_\pi((s_j, a_j), \tilde{Y}_k)$

PeerCT

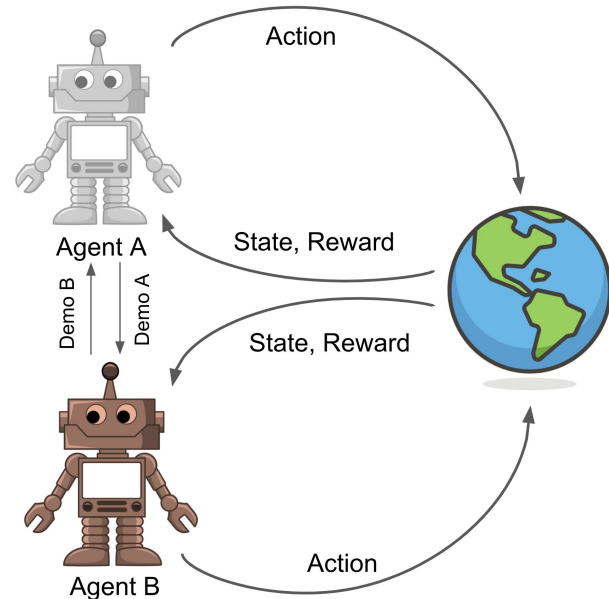


Policy Co-Training (Song et al., 2019) is an instance of hybrid policy learning

- Two agents A,B with policies π^A and π^B that receive partial observations
- Agents are trained jointly to learn with rewards and noisy demonstrations from each other.
- For instance, consider agent A
 - Besides interacting with environment, A also receives $\{s_i, \pi_B(s_i)\}$ from agent B
 - We consider π^B as the noisy version of the optimal policy

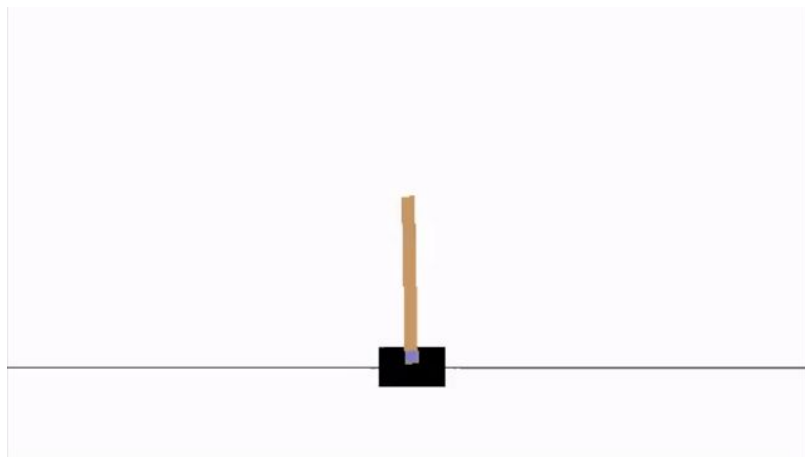
Similar to the PeerBC setting, we use CA with weak supervision to handle the noise in imperfect demonstrations

$$J^{\text{CT}}(\pi_\theta) = \mathbb{E} \left[\text{Eva}_\pi^{\text{RL}}((s_i^A, a_i^A), r_i^A) + \text{Eva}_\pi^{\text{BC}}((s_i^A, a_i^A), a_i'^B) \right] \\ - \xi \cdot \mathbb{E} \left[\text{Eva}_\pi^{\text{BC}}((s_j^A, a_j^A), a_k'^B) \right]$$

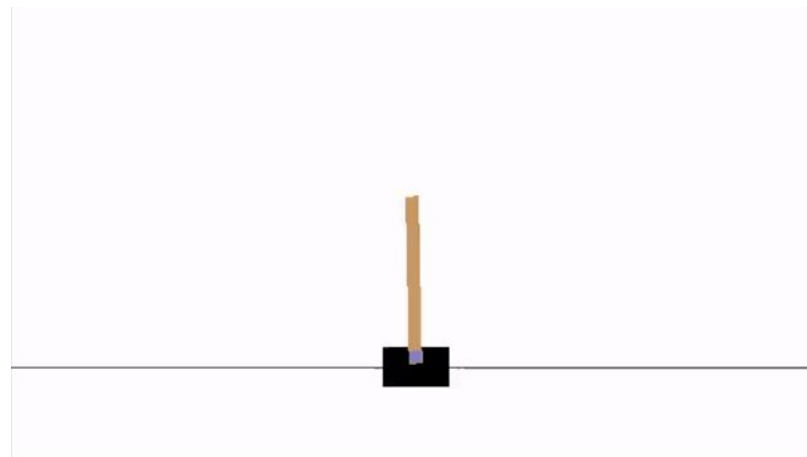


An example of PeerRL on CartPole

- RL with Noisy Rewards ($e_- = e_+ = 0.4$)
- training 10,000 frames using Dueling-DQN



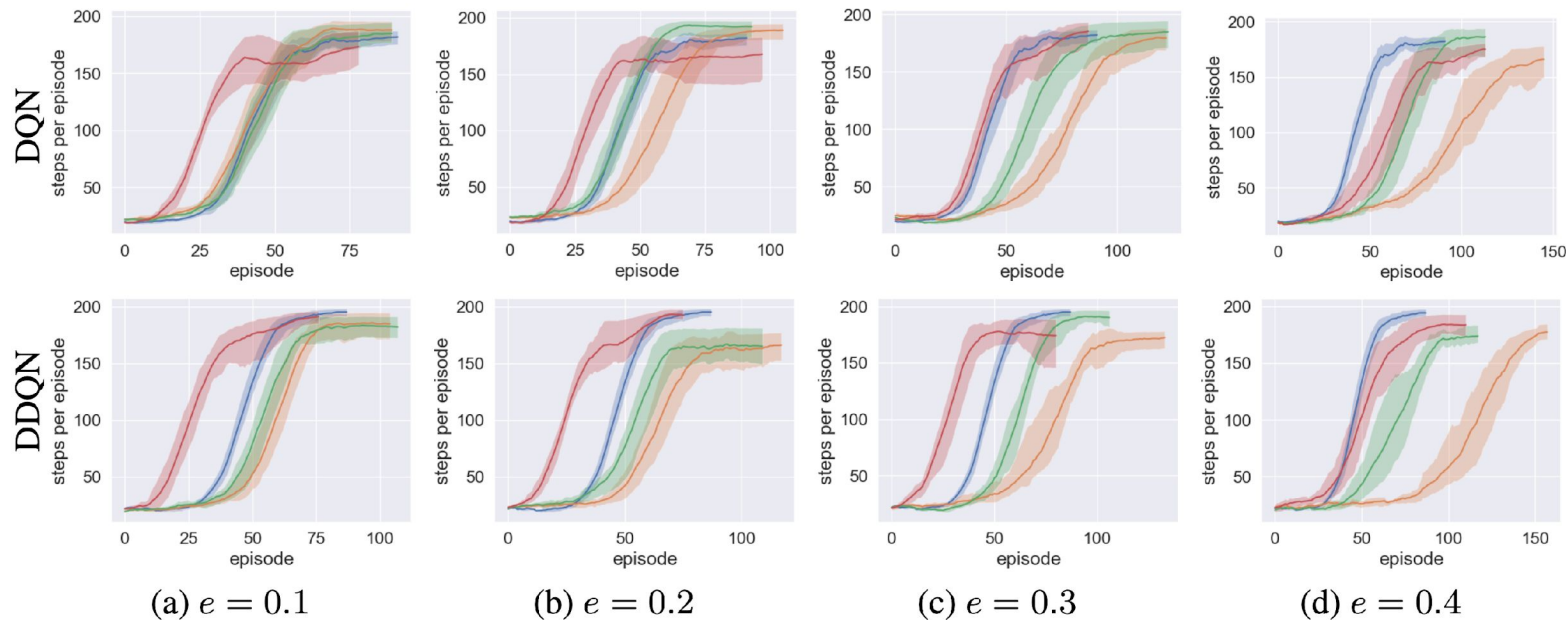
noisy reward \tilde{r}



peer reward \tilde{r}_{peer}

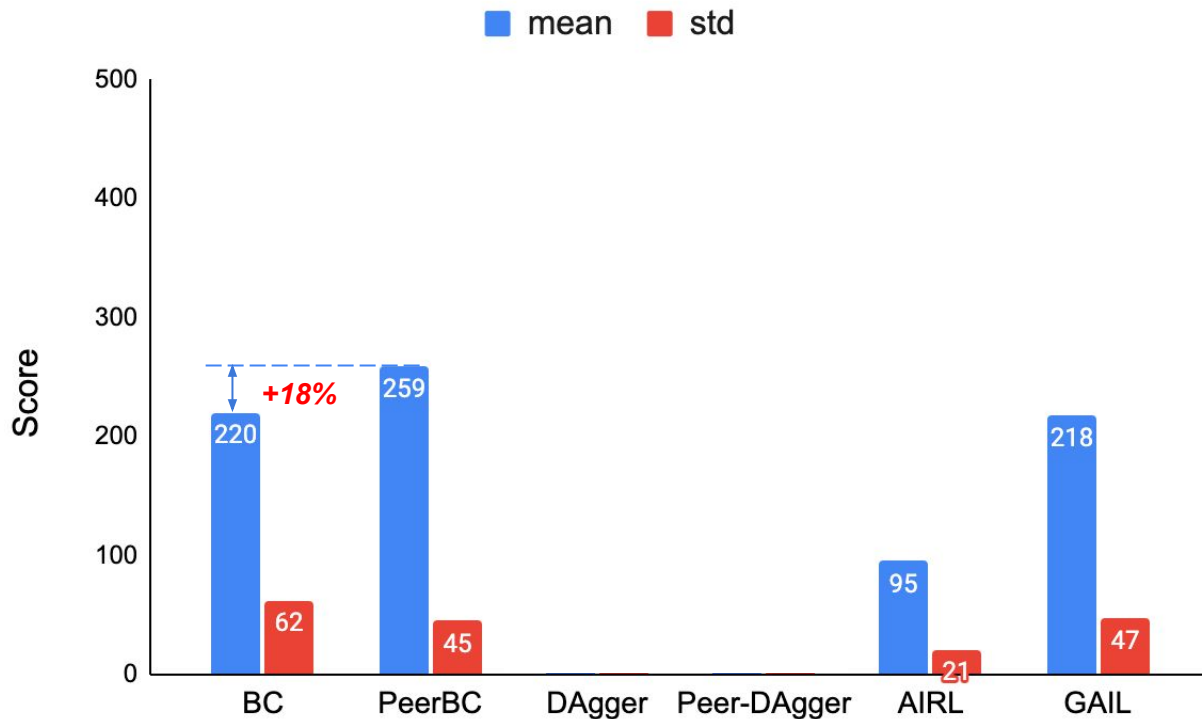
PeerRL recovers true reward signals

- **CartPole**: training DDQN for 10,000 steps on, binary reward: $\{-1, 1\}$
- symmetric noise: $e = e_- = e_+$



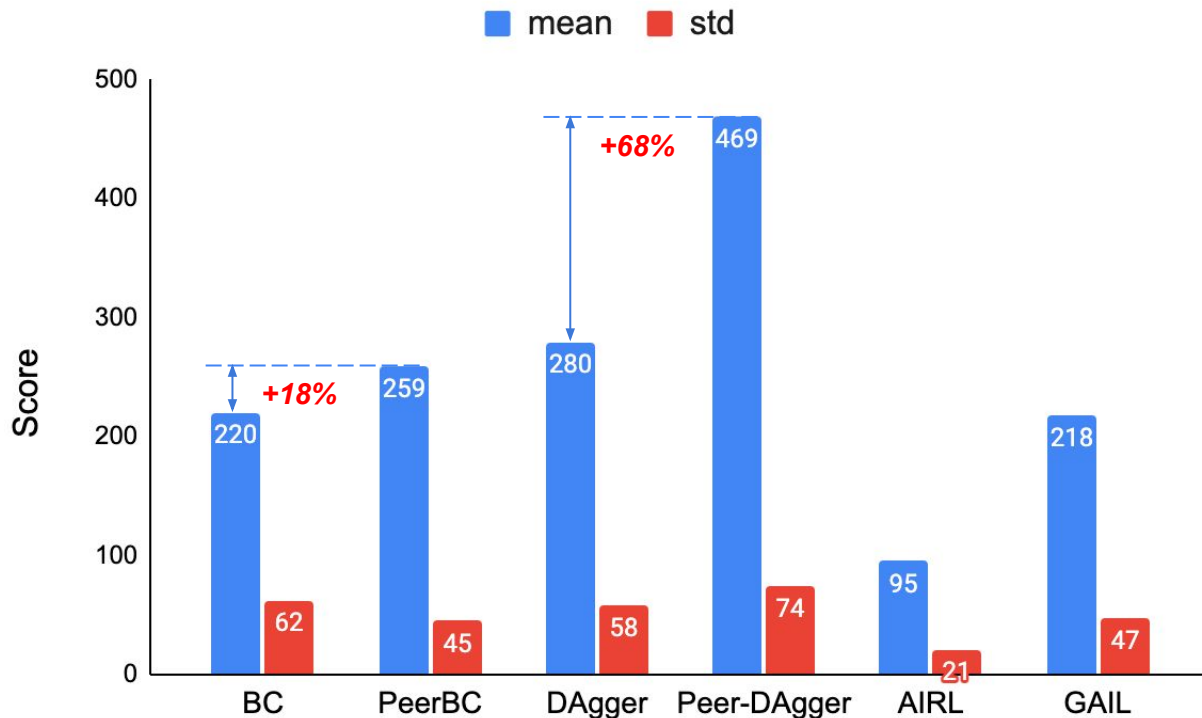
PeerBC recovers true expert signals

- *CartPole-v1*: train an imperfect RL model with PPO algorithm, unroll 16 episodes



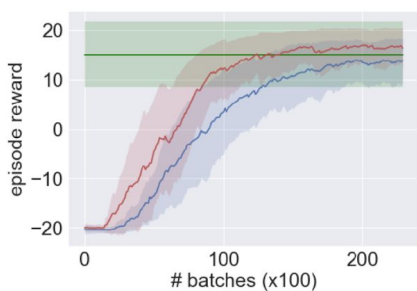
PeerBC recovers true expert supervision signals

- *CartPole-v1*: train an imperfect RL model with PPO algorithm, unroll 16 episodes

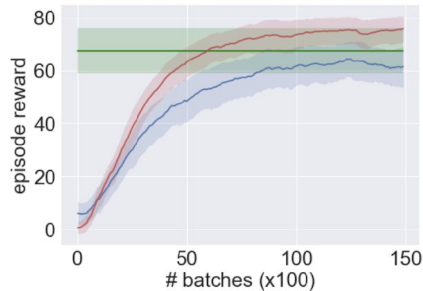


PeerBC recovers true expert signals

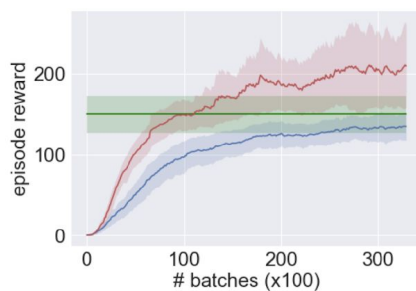
- **Atari games:** train an imperfect RL model with PPO algorithm
- weak expert = 70%~90% as good as fully converged agent
- collect demonstrations using weak expert and generate 100 trajectories for each environment
- Note that **no synthetic noise is added** in the experiments



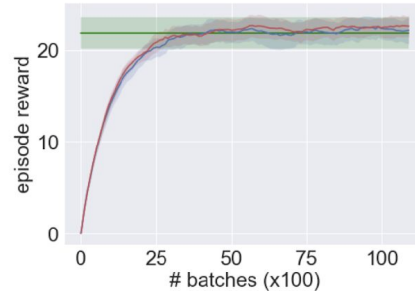
(a) Pong



(b) Boxing



(c) Enduro



(d) Freeway

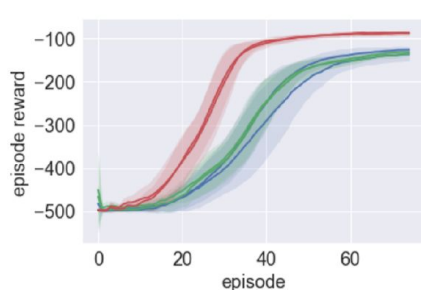
Standard BC

Weak expert

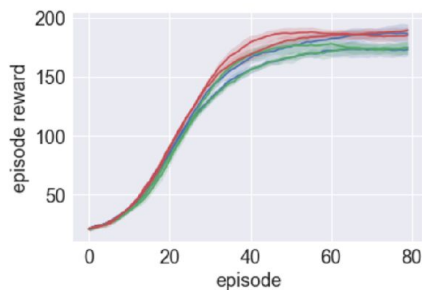
PeerBC (ours)

PeerCT recovers true reward signals

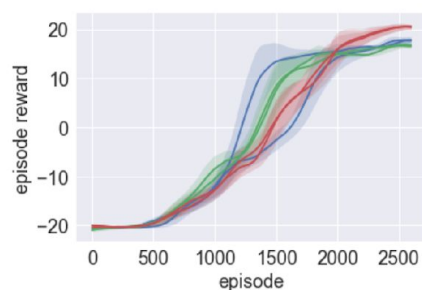
- **Continuous Control/Atari:** adopt the exact same setting as Song et al., 2019 **without any synthetic noise included**
- removes all even index coordinates in the state vector (view-A) or removing all odd index ones (view-B)
- implies the potential of our approach to deal with natural noise in real-world applications



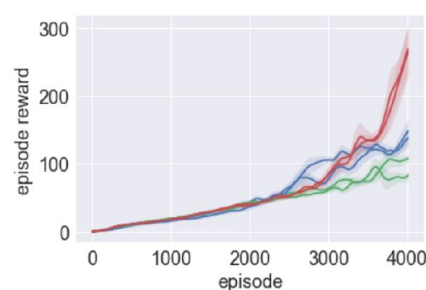
(a) Acrobot



(b) CartPole



(c) Pong



(d) Breakout

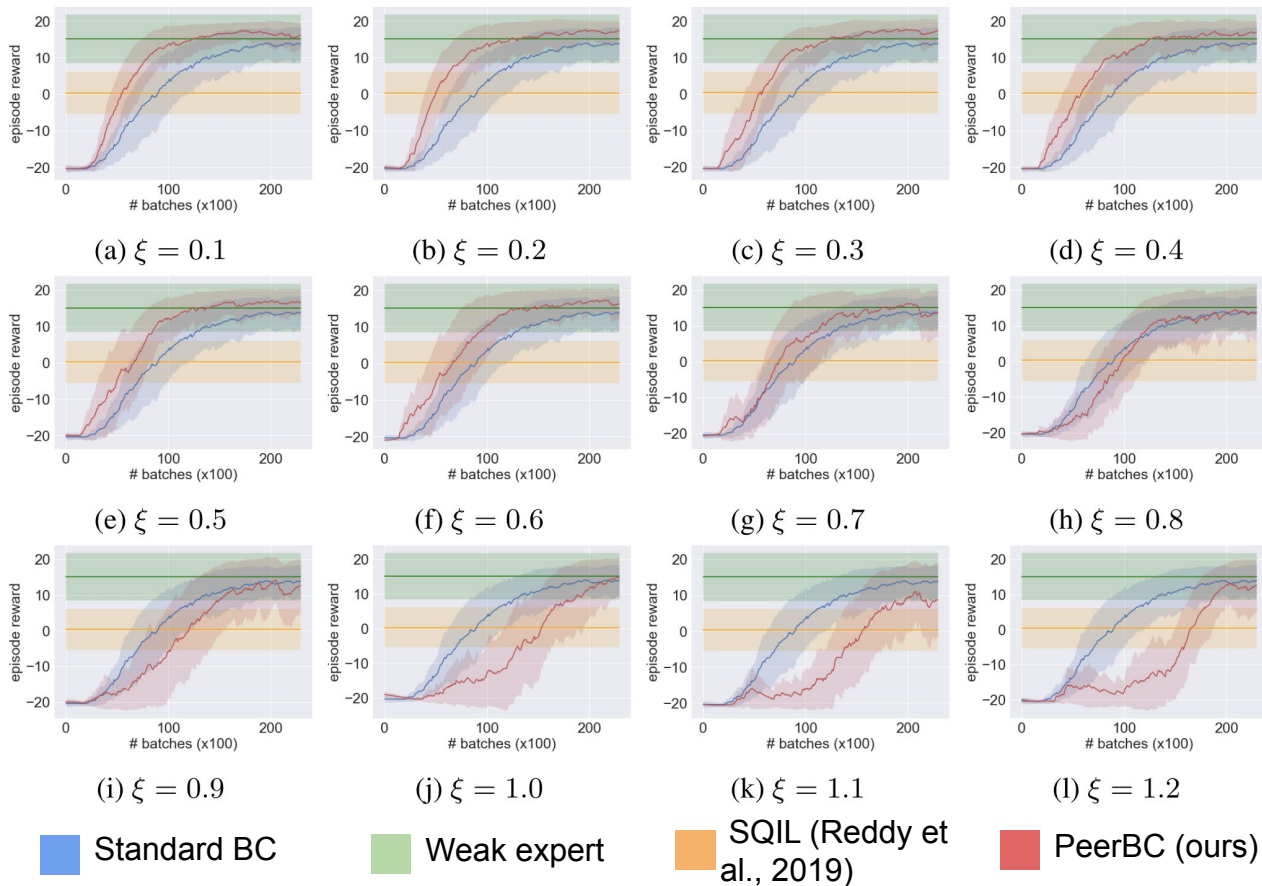
Single view

Co-Training
(Song et al., 2019)

Peer Co-Training (ours)

Sensitivity of over-agreement penalty

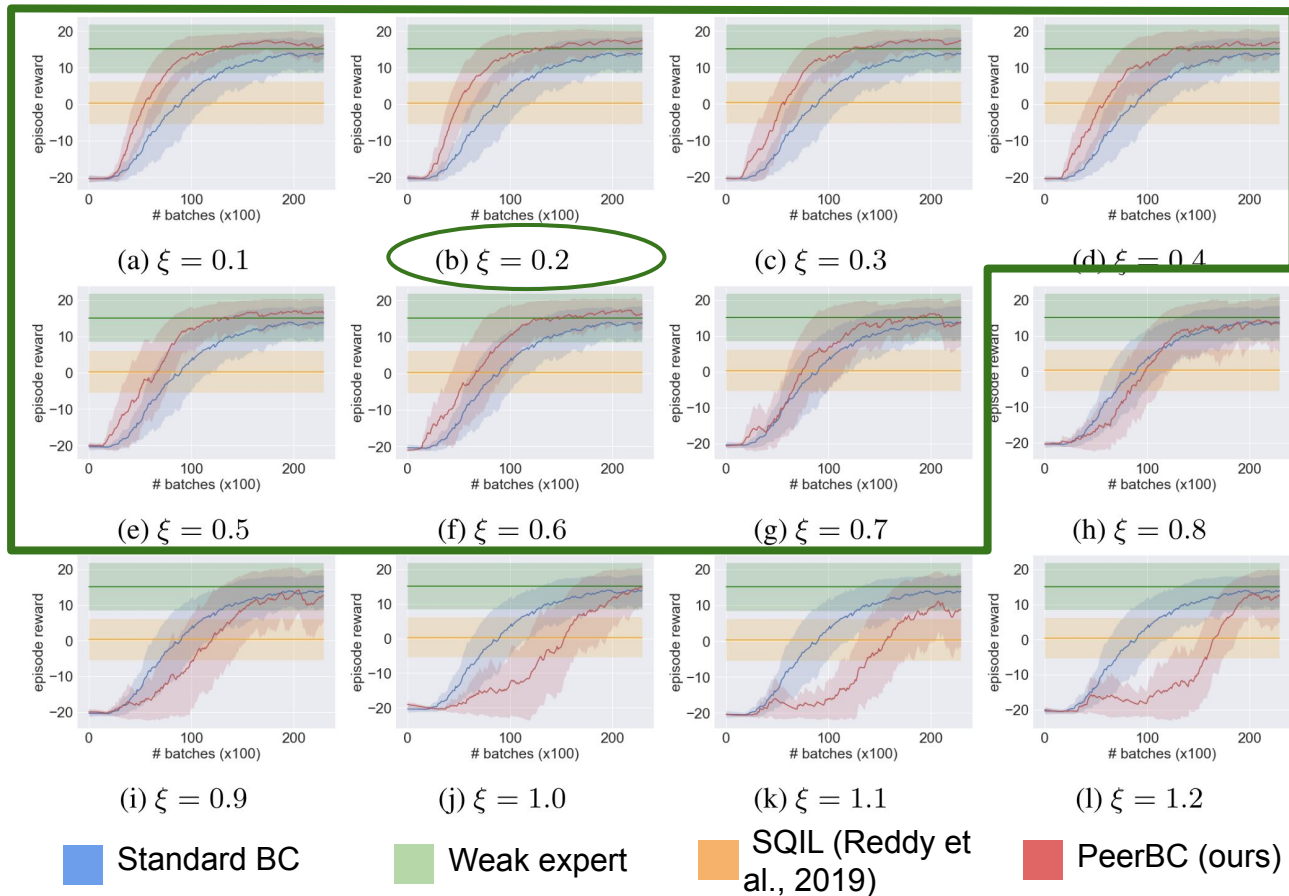
Atari - Pong



Sensitivity of over-agreement penalty

Atari - Pong

Our method works robustly
in a wide range of ξ !

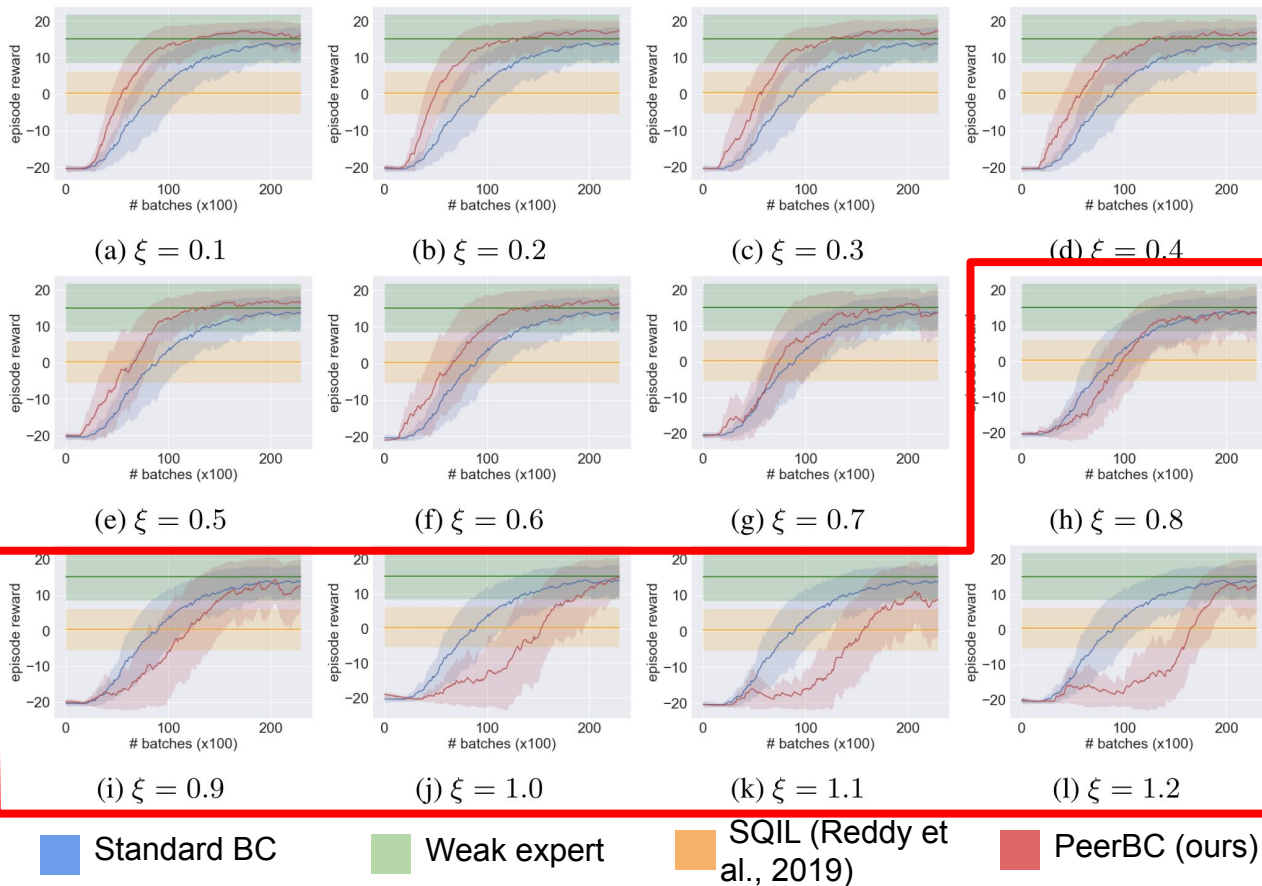


Sensitivity of over-agreement penalty

Atari - Pong

Our method works robustly in a wide range of ξ !

Overly large penalty introduces too much noise



Conclusion

- We provided a unified formulation of the *weakly supervised policy learning* problems
- We proposed PeerPL, a weakly supervised policy learning framework to **unify a series of RL/BC problems with low-quality supervision signals**
 - RL with perturbed reward
 - BC with imperfect demonstrations
 - Policy Co-Training (Hybrid RL + BC)
- Our method is **theoretically guaranteed to recover the optimal policy** with sufficient weak supervision signals.