

# VAST: Value Function Factorization with Variable Agent Sub-Teams

## NeurIPS 2021

Thomy Phan<sup>1</sup>, Fabian Ritz<sup>1</sup>, Lenz Belzner<sup>2</sup>,  
Philipp Altmann<sup>1</sup>, Thomas Gabor<sup>1</sup>, Claudia Linnhoff-Popien<sup>1</sup>

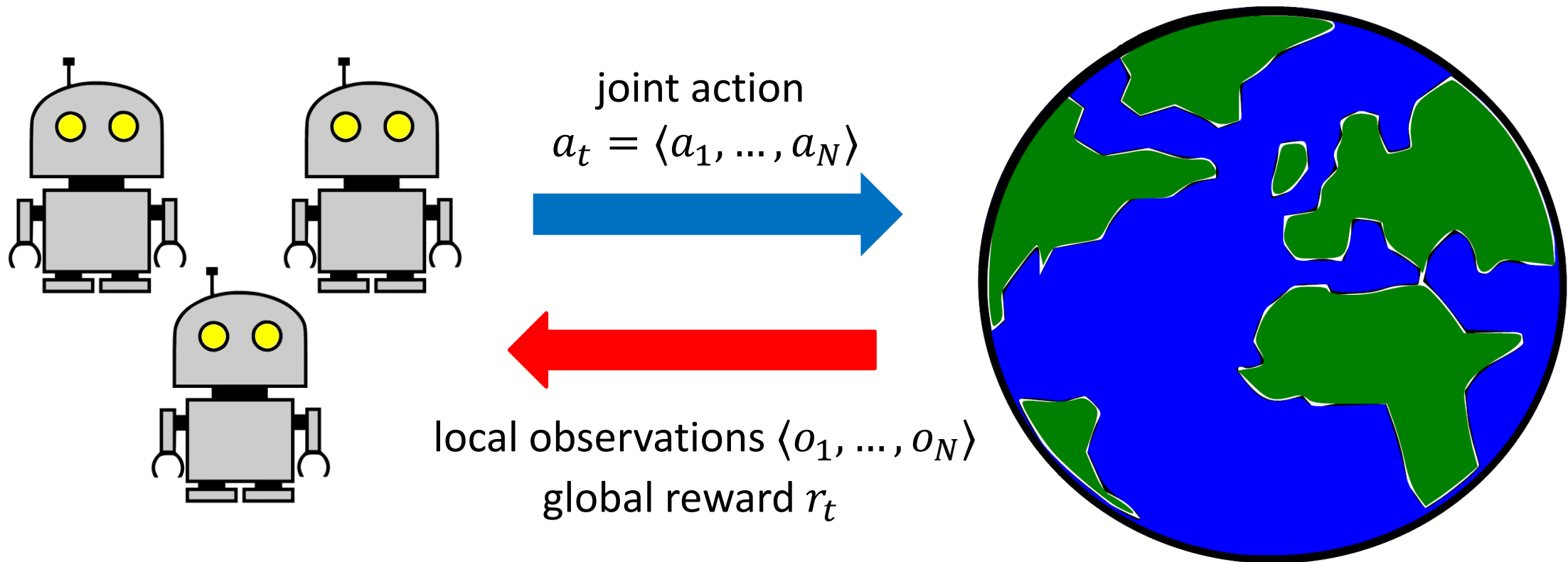
<sup>1</sup>LMU Munich, <sup>2</sup>Technische Hochschule Ingolstadt



# Preliminaries

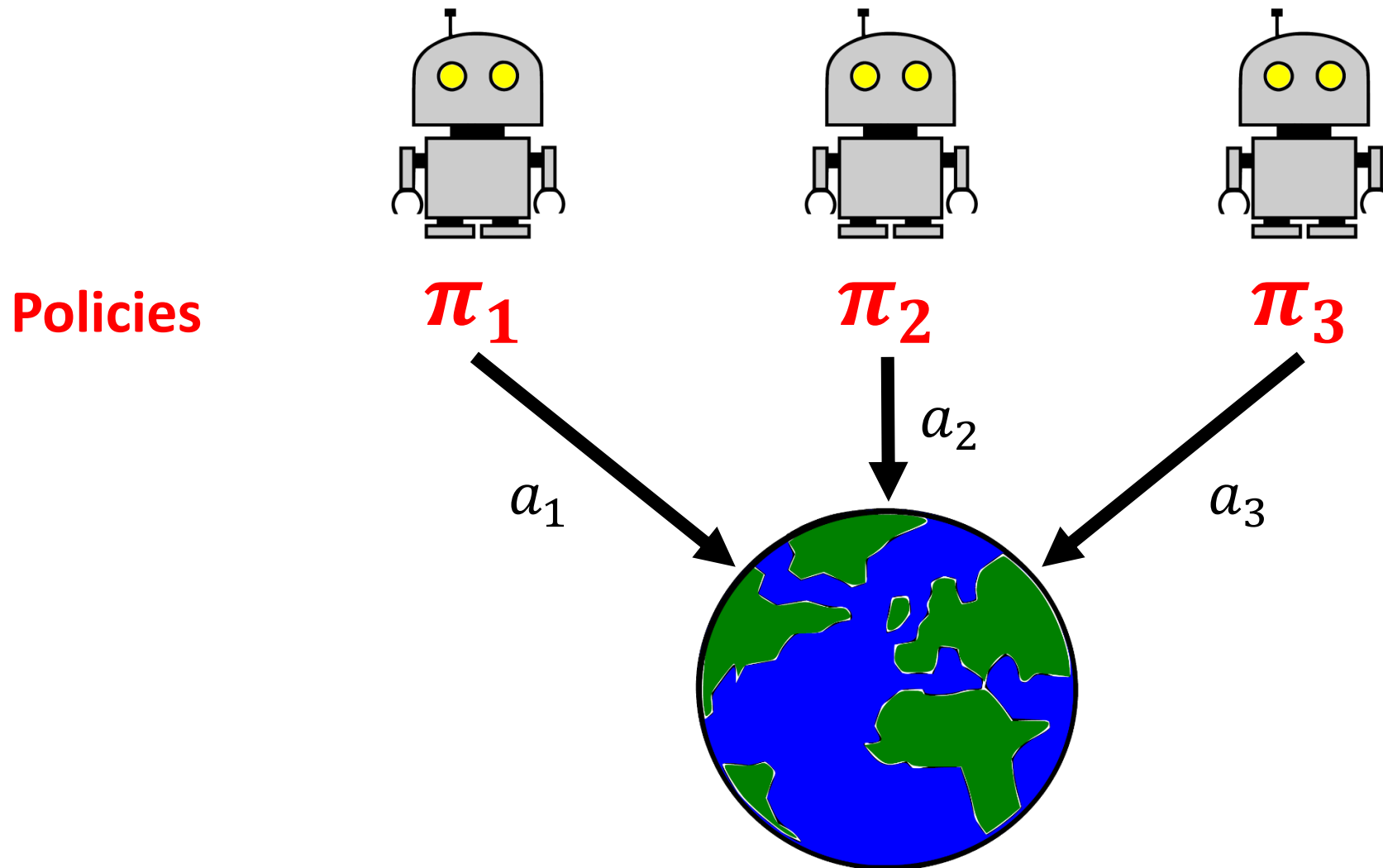


# Cooperative Multi-Agent Systems (MAS)

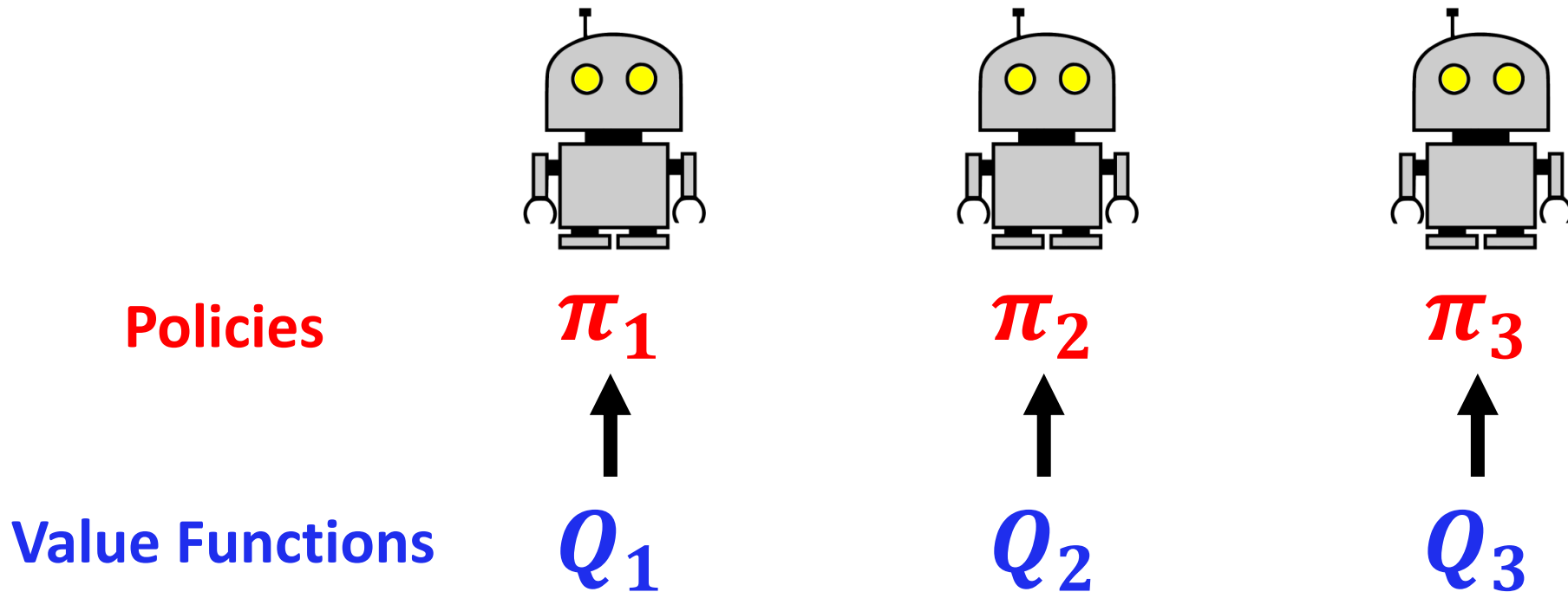


**Goal:** Maximize expectation of the return  $\sum_{k=1}^{\infty} \gamma^k r_{t+k}$

# Multi-Agent Reinforcement Learning



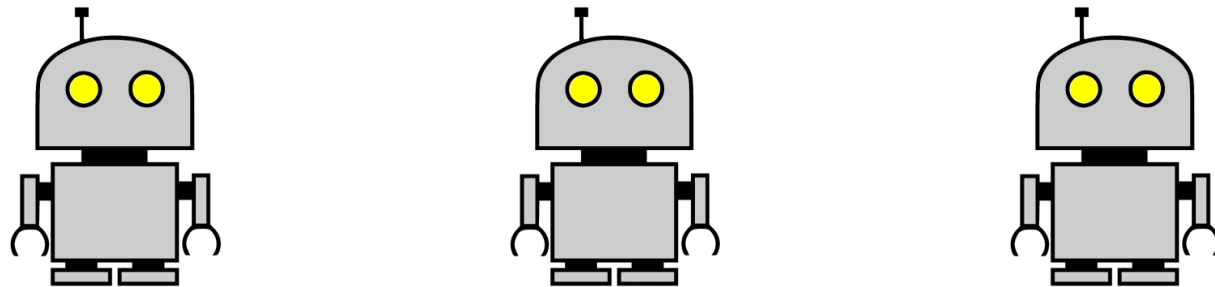
# Value-based Multi-Agent Reinforcement Learning



$$Q_i(\tau_i, a_i) = \mathbb{E}\left[\sum_{k=1}^{\infty} \gamma^k r_{t+k}\right]$$

# Value Function Factorization

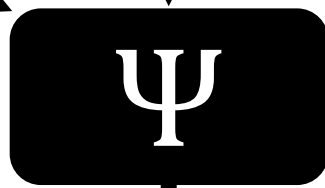
Local  
Value Functions



$Q_1$

$Q_2$

$Q_3$



Factorization Operator

Centralized  
Value Function

$$Q_{tot} = \mathbb{E}[\sum_{k=1}^{\infty} \gamma^k r_{t+k}]$$

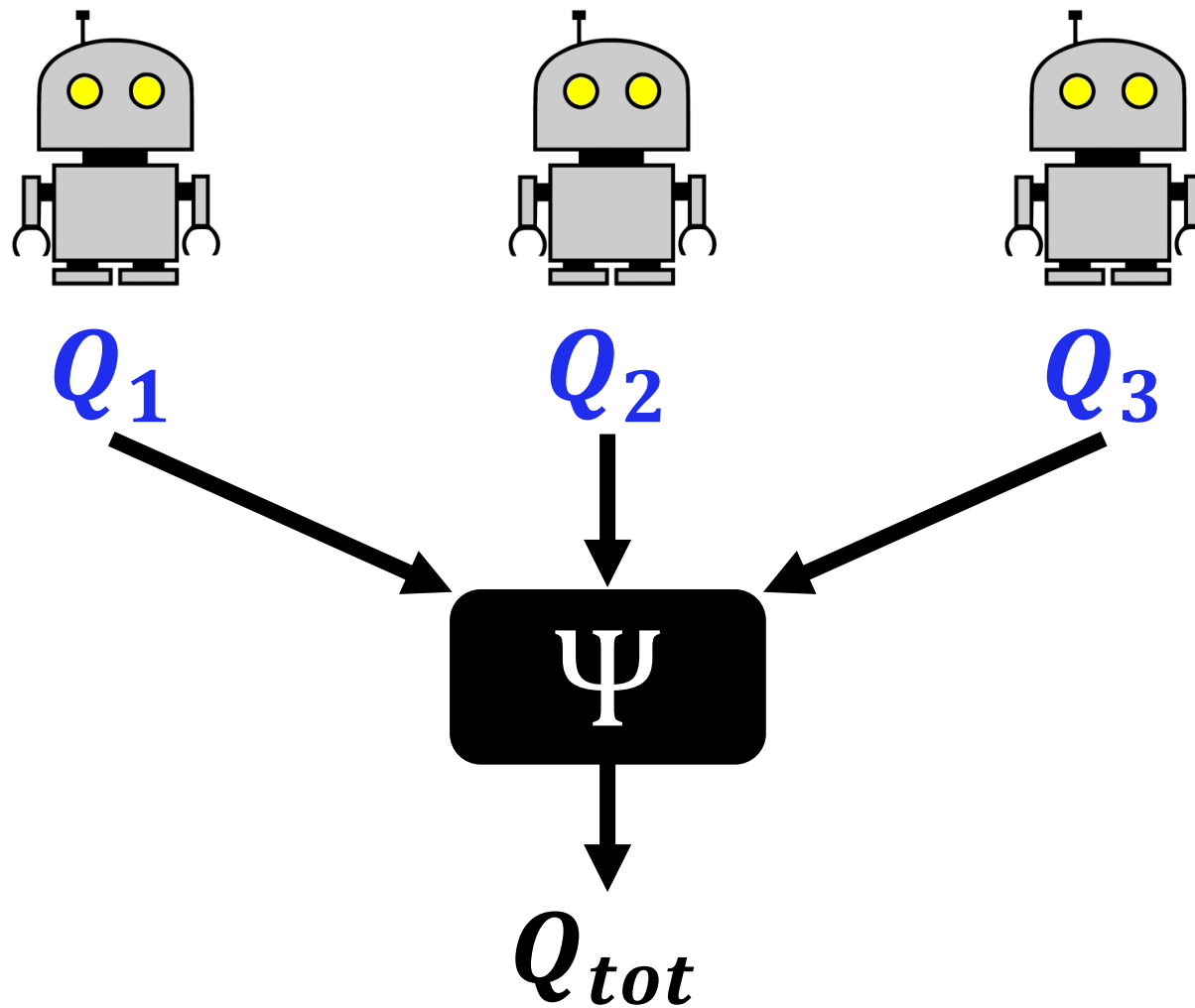
- VDN
- QMIX
- QTRAN
- W-QMIX
- Qatten
- QPLEX
- ...

# Individual-Global-Max (IGM) Consistency

$$\operatorname{argmax}_{\mathbf{a}_t} \mathbf{Q}_{tot}(\boldsymbol{\tau}_t, \mathbf{a}_t) = \begin{pmatrix} \operatorname{argmax}_{a_{t,1}} Q_1(\tau_{t,1}, a_{t,1}) \\ \dots \\ \operatorname{argmax}_{a_{t,N}} Q_N(\tau_{t,N}, a_{t,N}) \end{pmatrix}$$

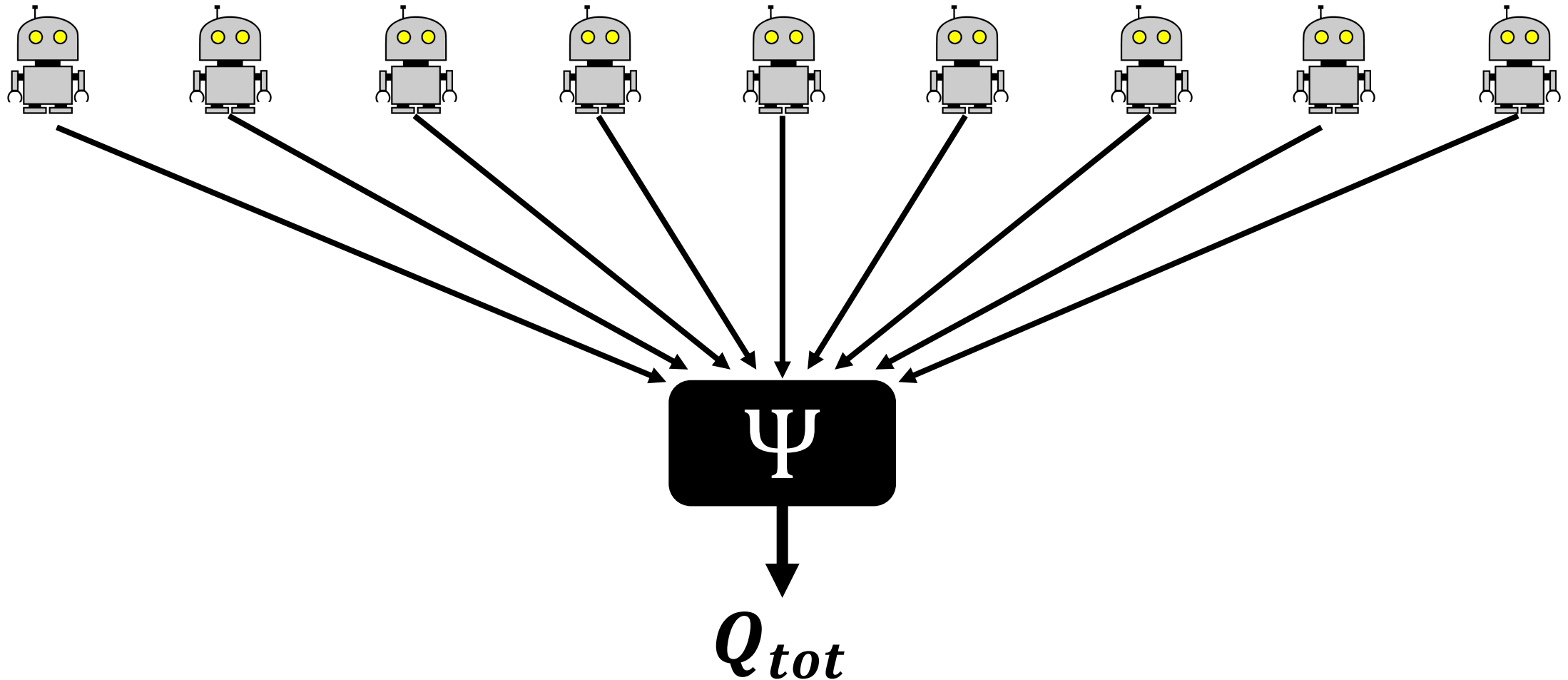
Factorization operators must ensure IGM consistency

# Scalability of Value Function Factorization

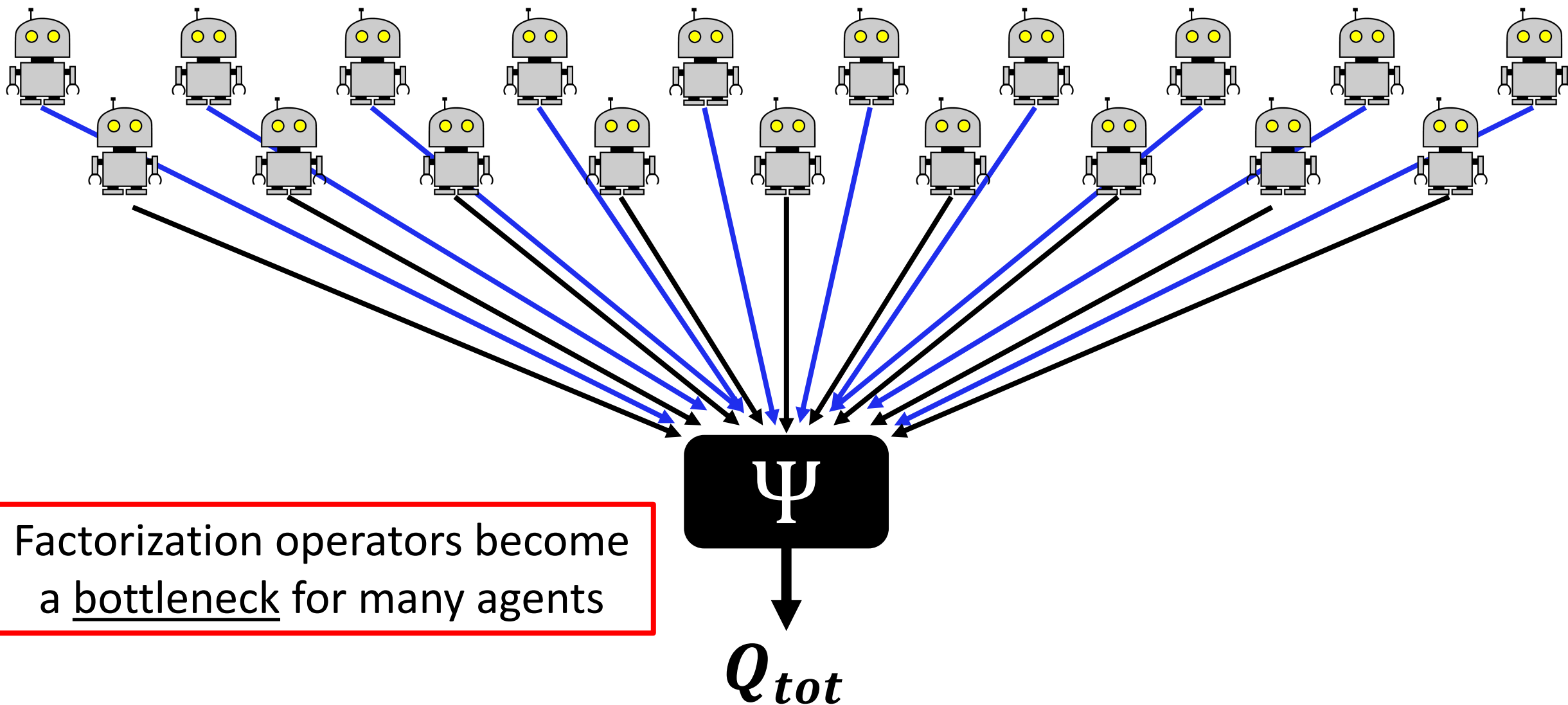




# Scalability of Value Function Factorization



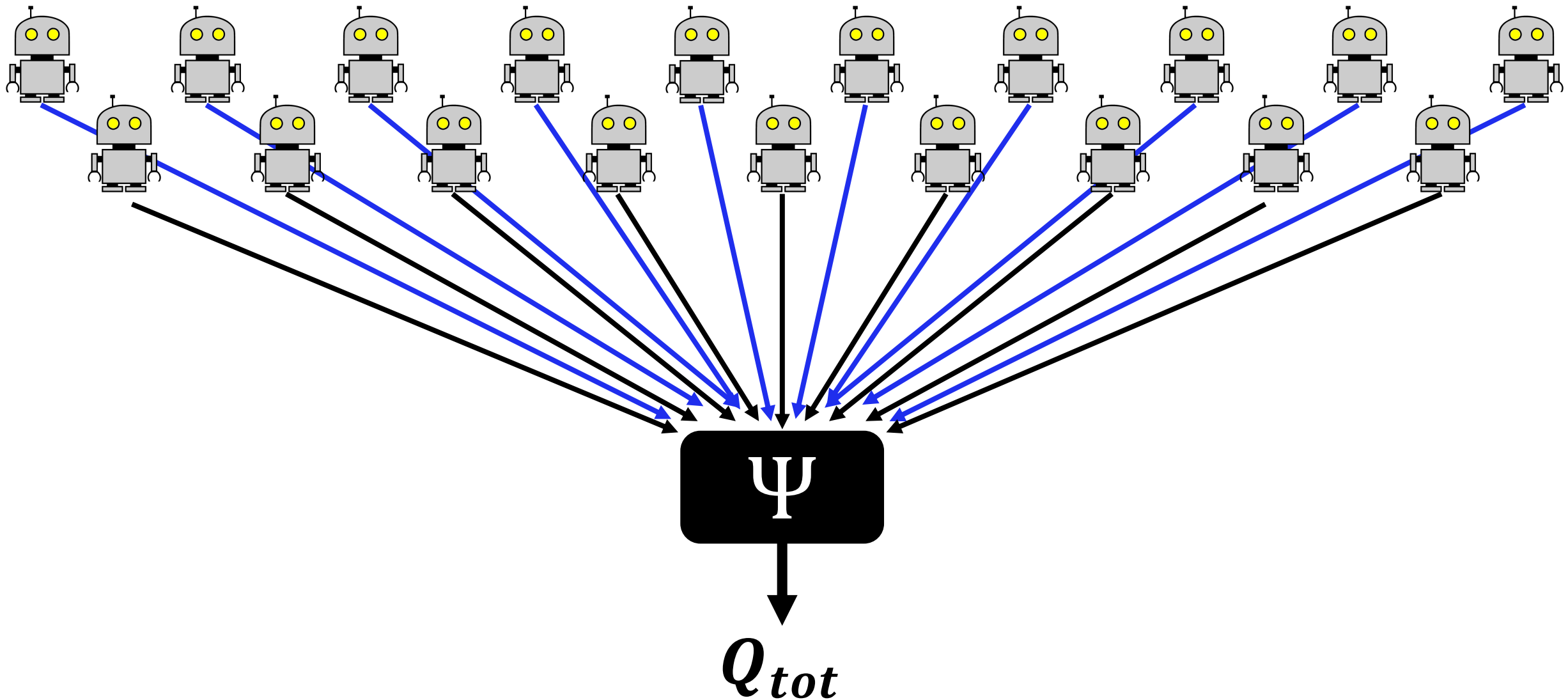
# Scalability of Value Function Factorization



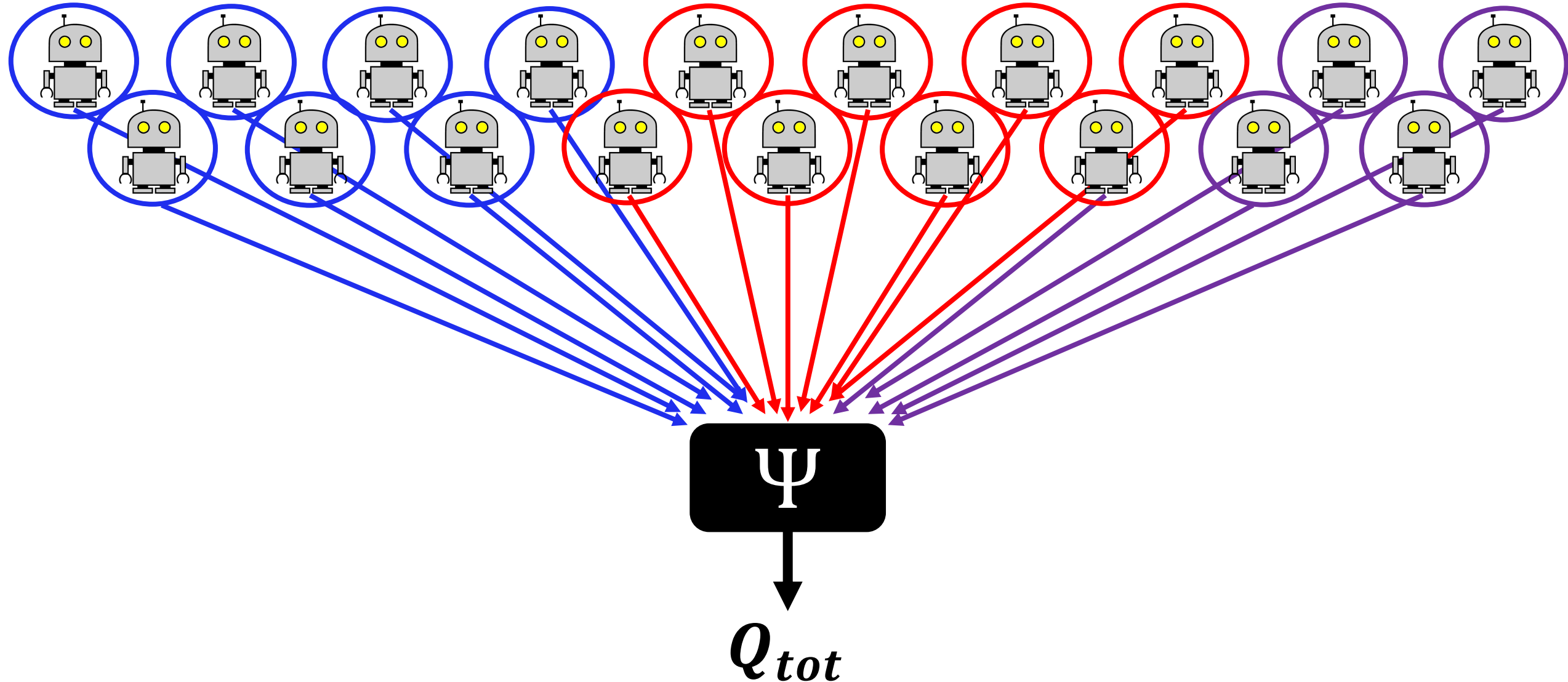
# Value Function Factorization with Variable Agent Sub-Teams (VAST)



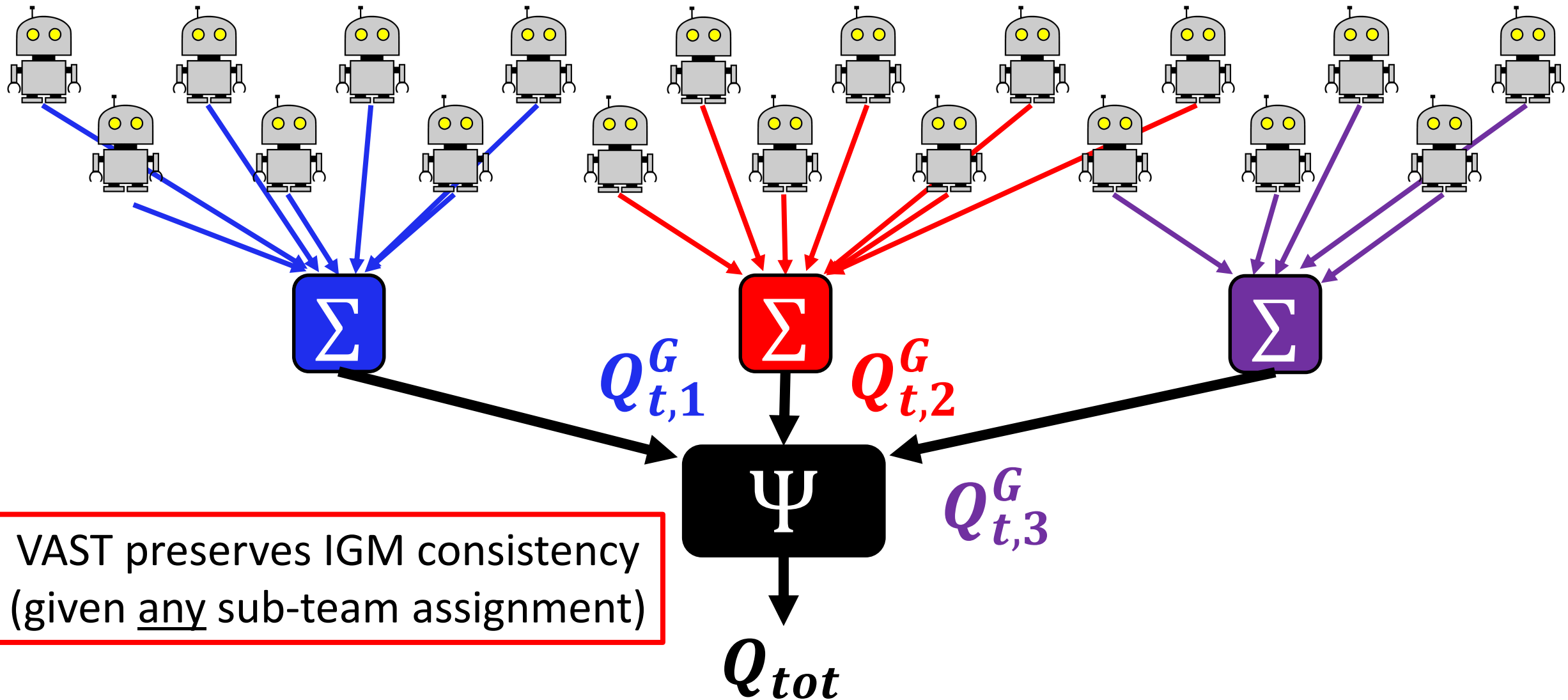
# Idea of VAST



# Idea of VAST: Sub-Team Assignment



# Idea of VAST: Factorization on Sub-Team Values



VAST preserves IGM consistency (given any sub-team assignment)

# Meta-Gradient Learning for Sub-Team Assignment

- **Idea:** Optimize sub-team assignments using a high-level objective  $J$ 
  - Decide at each state  $s_t$  which sub-team  $k$  agent  $i$  should be assigned to
  - Learn meta-policy  $\mathcal{X}(k|s_t, i, \tau_{t,i})$  via gradient ascent w.r.t. objective  $J$

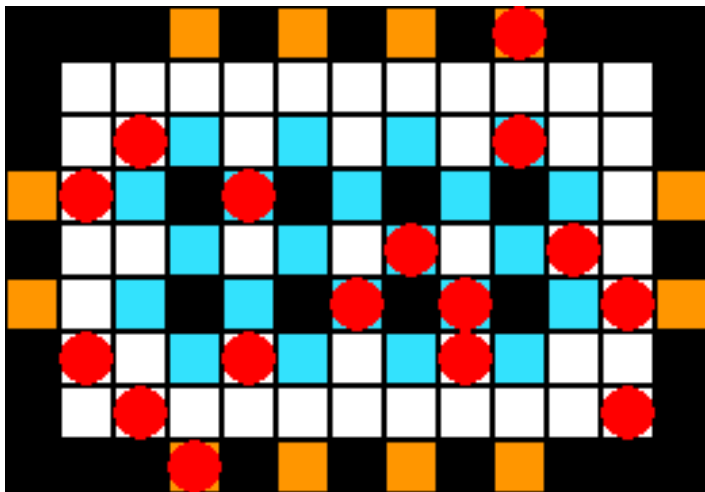
$$\hat{A}(k, i, s_t, \tau_{t,i}) \nabla \log \mathcal{X}(k|s_t, i, \tau_{t,i})$$

- Advantage function  $\hat{A}$  can be defined using domain knowledge or reward-based metrics (e.g., return, TD-error, ...)

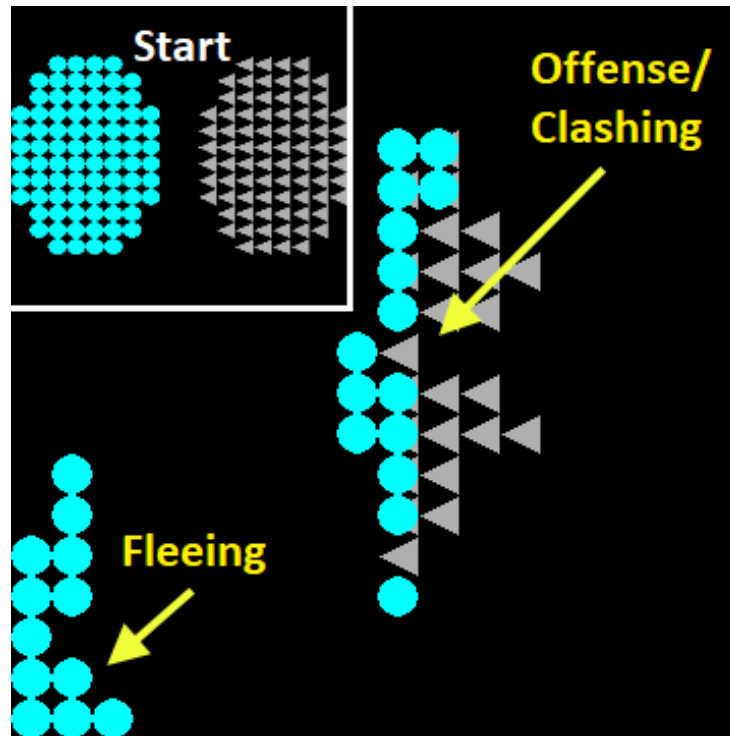
# Results



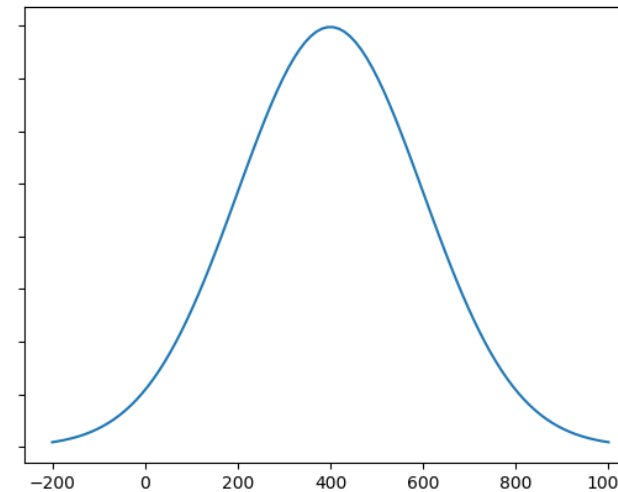
# Evaluation Domains



**Warehouse**  
(4 – 16 agents)

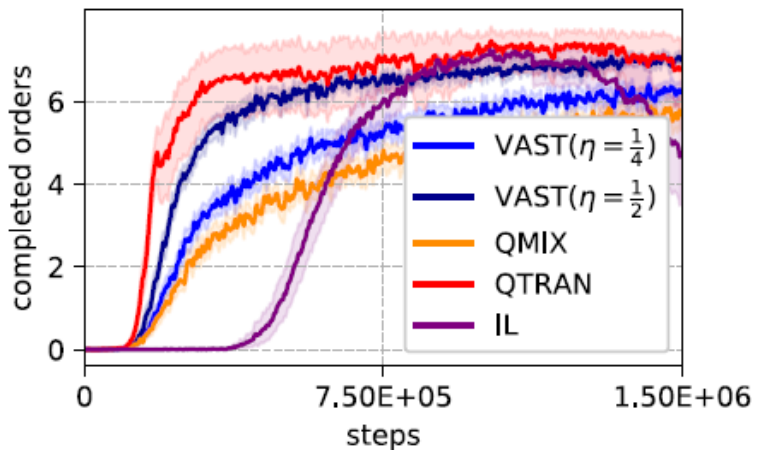


**Battle**  
(20 – 80 agents)

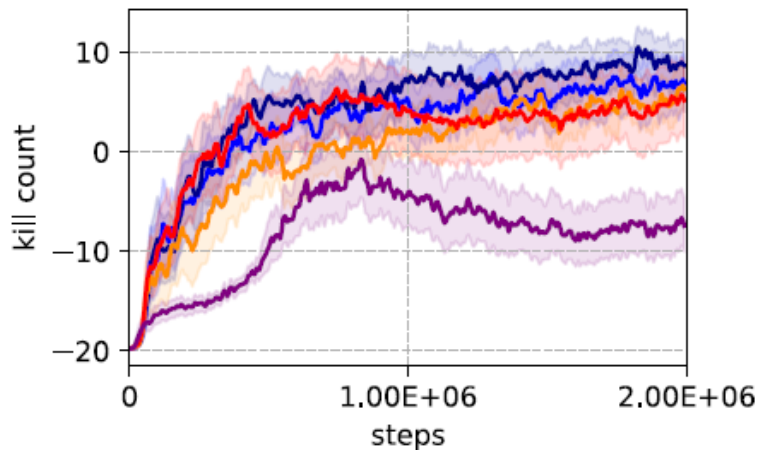


**Gaussian Squeeze**  
(200 – 800 agents)

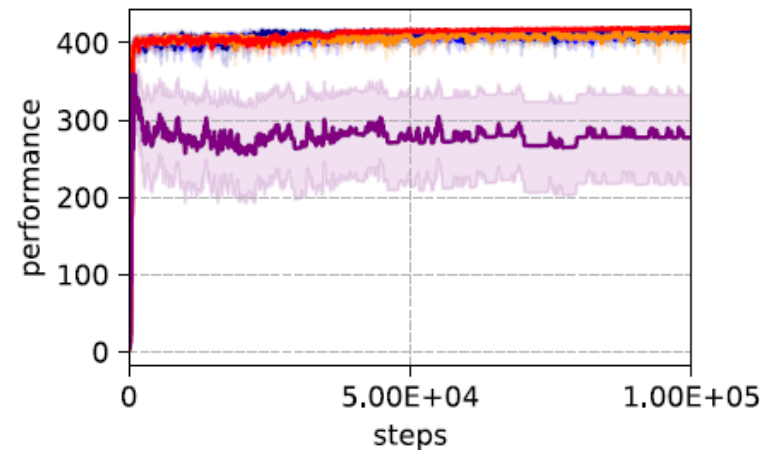
# State-of-the-Art Comparison



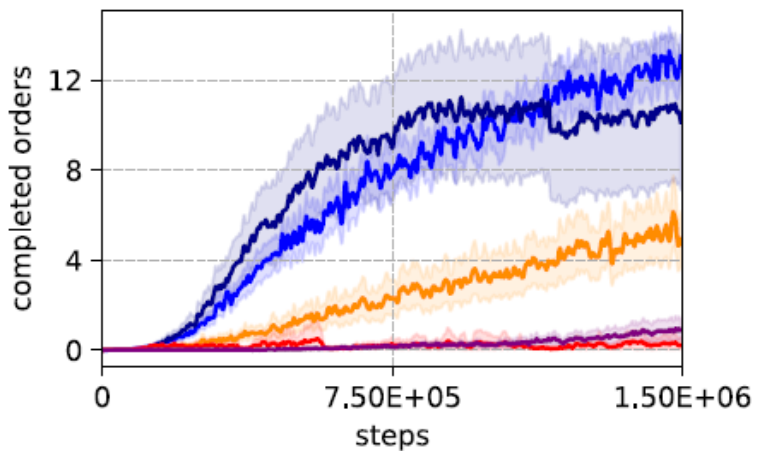
(a) *Warehouse[4]*



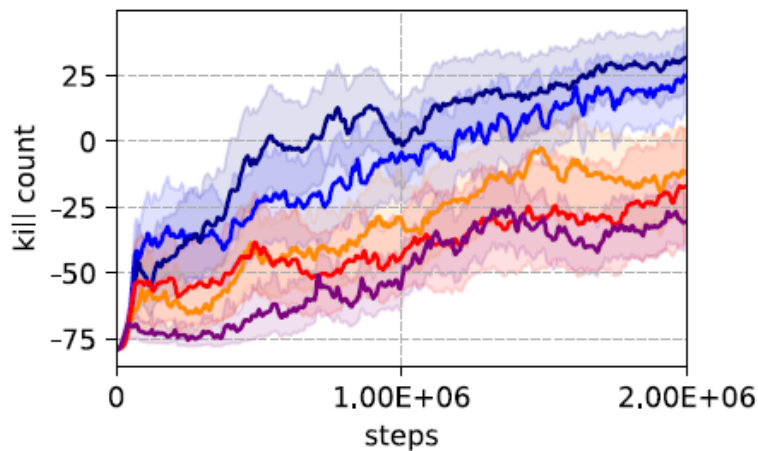
(b) *Battle[20]*



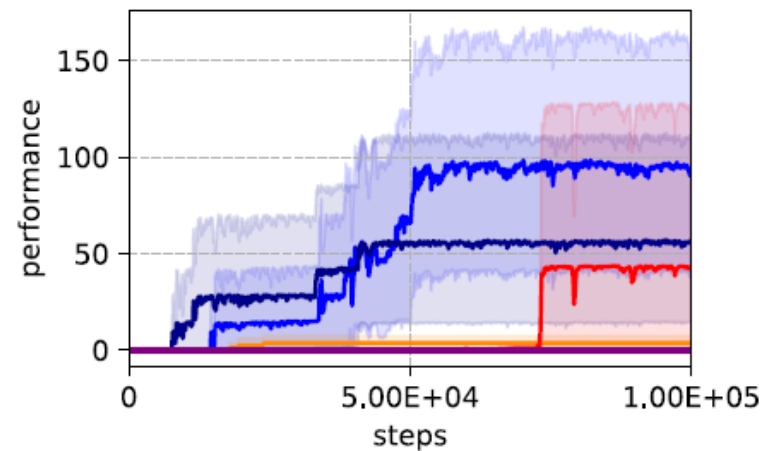
(c) *GaussianSqueeze[200]*



(d) *Warehouse[16]*

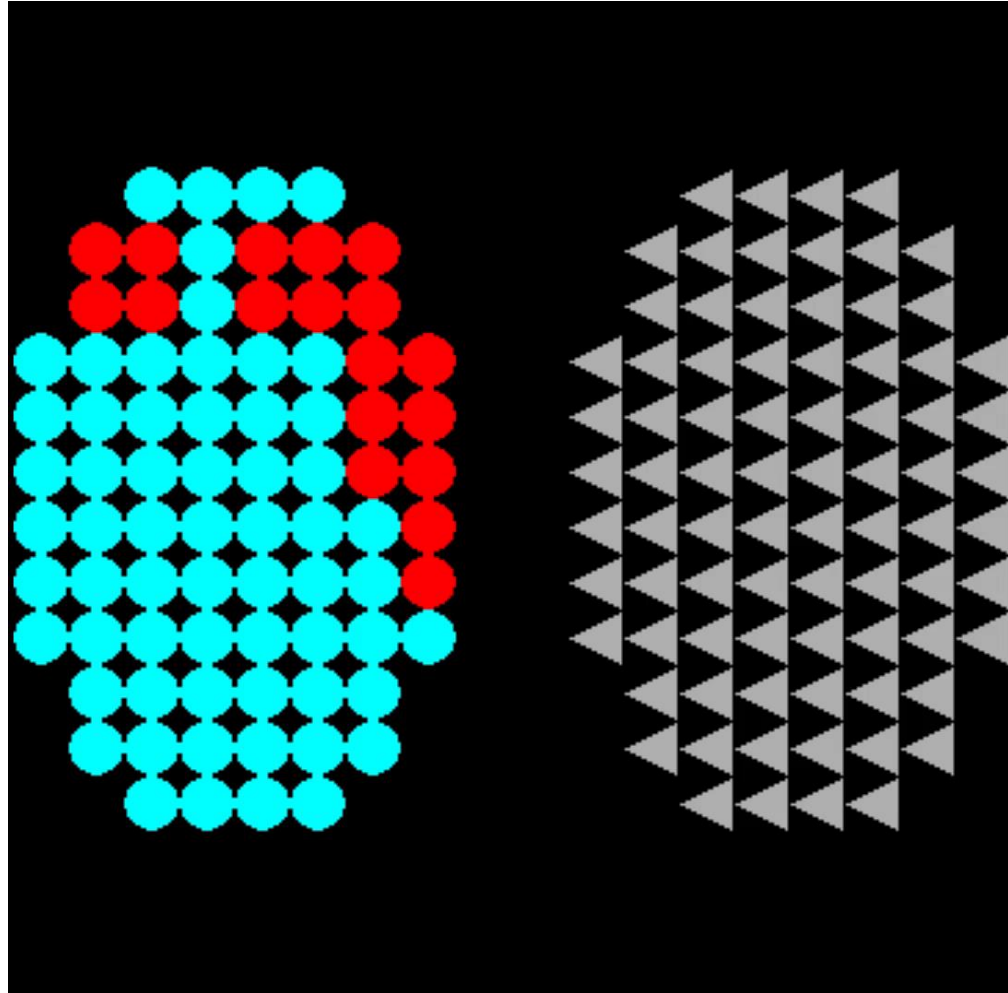


(e) *Battle[80]*

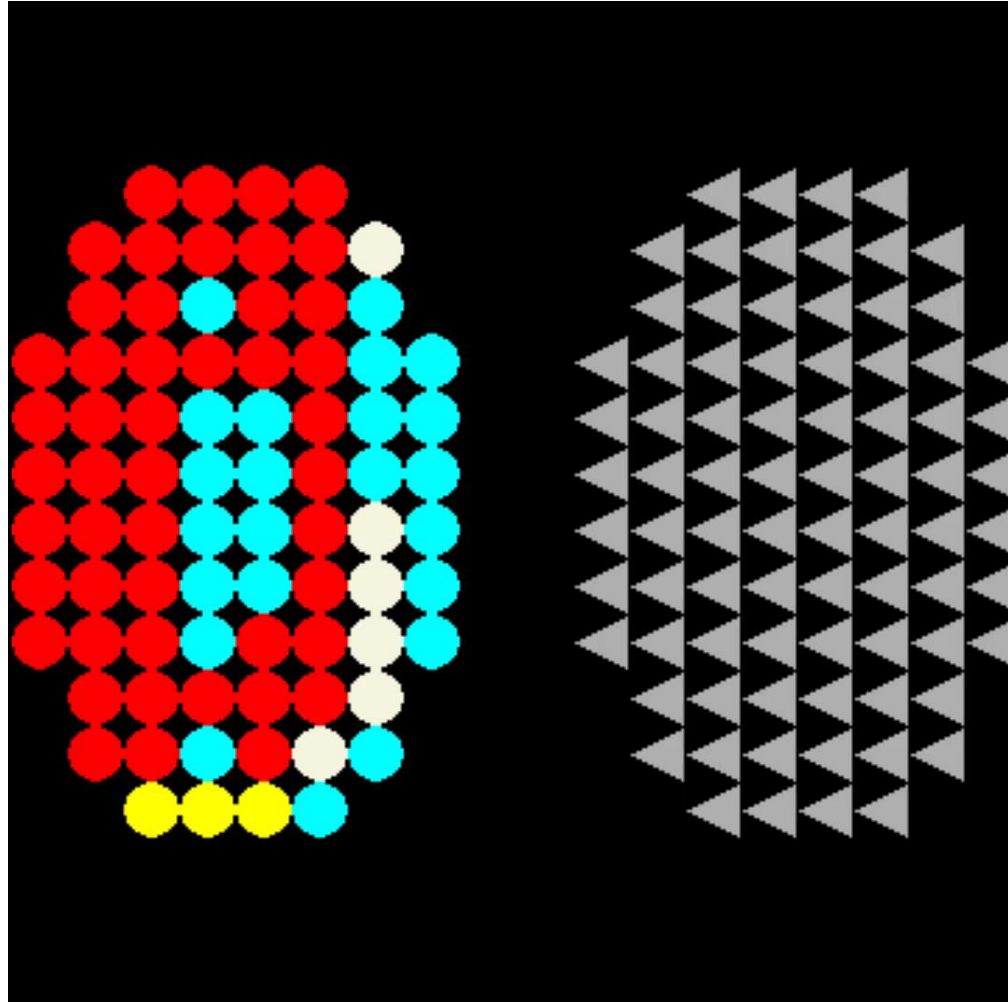


(f) *GaussianSqueeze[800]*

# Meta-Gradient Generated Sub-Teams in Battle[80]



# Meta-Gradient Generated Sub-Teams in Battle[80]



# Conclusion

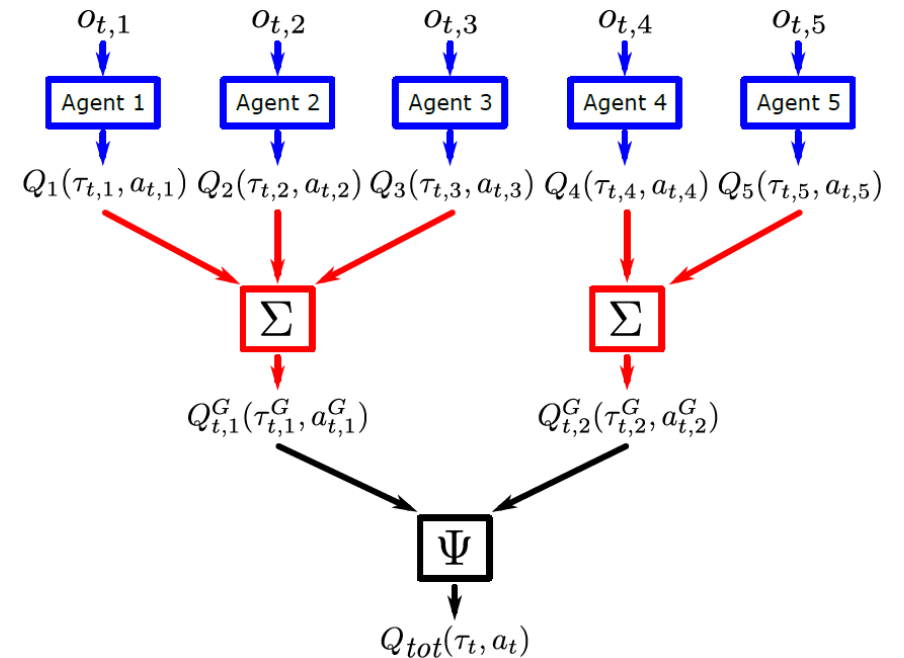


# Conclusion and Future Work

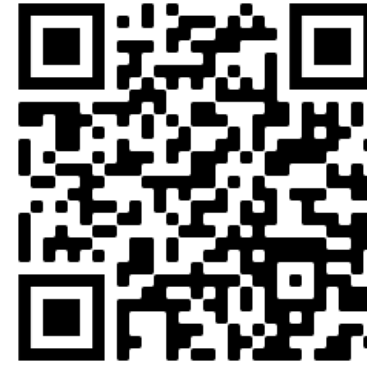
- VAST can improve scalability of value factorization w.r.t. many agents
- IGM consistency is preserved by VAST
- Meta-gradient based sub-teams can improve performance of VAST

## Future Work

- Deeper hierarchies of sub-teams
- Non-linear factorization of sub-team values



Code available at 



# VAST: Value Function Factorization with Variable Agent Sub-Teams

## NeurIPS 2021

Thomy Phan<sup>1</sup>, Fabian Ritz<sup>1</sup>, Lenz Belzner<sup>2</sup>,  
Philipp Altmann<sup>1</sup>, Thomas Gabor<sup>1</sup>, Claudia Linnhoff-Popien<sup>1</sup>

<sup>1</sup>LMU Munich, <sup>2</sup>Technische Hochschule Ingolstadt

