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# Combinatorial Optimization for Panoptic Segmentation: A Fully Differentiable Approach

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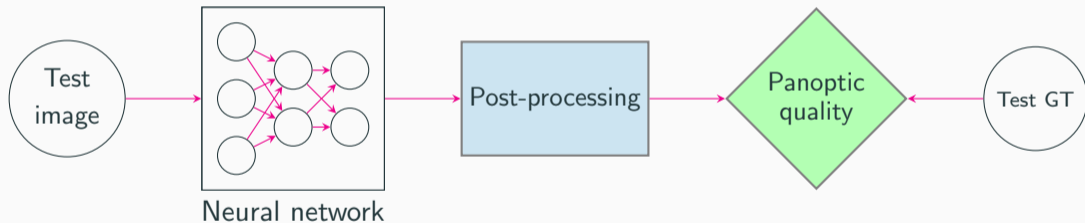
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# Panoptic segmentation = Semantic $\cup$ Instance seg.

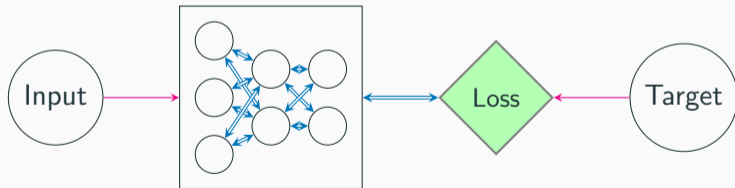


# Evaluation pipeline for panoptic segmentation



## Conventional training pipeline

- Post-processing block not part of training
- Test-time evaluation metric not used in training



## Existing methods

1. Do not optimize for panoptic labels
2. Require many parameters (e.g. loss balancing weights, post-processing)
3. Complex architecture (e.g. additional Mask-RCNN for ROI)

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## Our aims

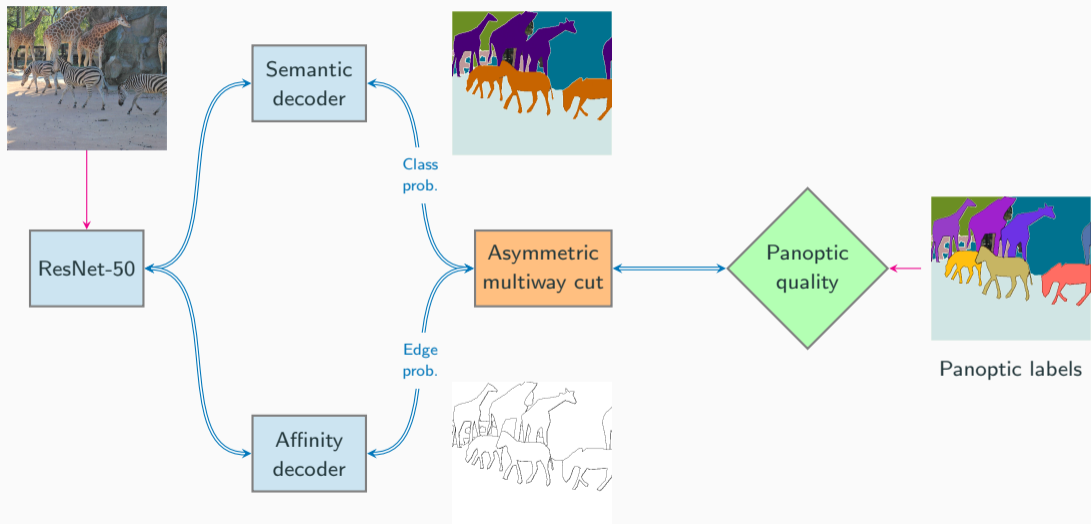
1. Fully differentiable pipeline
2. Optimize for the evaluation metric
3. Fewer hyperparameters
4. Use 'standard' neural network architecture (ResNet50)

# Literature review

Methods	Simplicity	Params.		End-to-end	Optimize PQ	Performance
		Train	Eval			
MaxDeepLab <sup>1</sup>	Red	Yellow	Red	Green	Yellow	Green
EfficientPS <sup>2</sup>	Red	Red	Red	Red	Red	Green
AxialDeepLab <sup>3</sup>	Yellow	Yellow	Yellow	Red	Red	Yellow
PanopticDeepLab <sup>4</sup>	Green	Yellow	Yellow	Red	Red	Yellow
UPNet <sup>5</sup>	Red	Red	Yellow	Red	Red	Yellow
SMW <sup>6</sup>	Green	Red	Green	Red	Red	Red
SSAP <sup>7</sup>	Green	Yellow	Green	Red	Red	Red
Our aim	Green	Yellow	Green	Green	Green	?

<sup>1</sup>Wang 2020b, <sup>2</sup>Mohan 2021, <sup>3</sup>Wang 2020a, <sup>4</sup>Cheng 2020, <sup>5</sup>Xiong 2019, <sup>6</sup>Wolf 2020, <sup>7</sup>Gao 2019

# Our pipeline





## Multiway cut (MWC) - Calinescu 2008

Generalization of graph-cut on  $G = (V, E)$  for  $K > 2$

$$\begin{aligned} \min_{\substack{x: V \rightarrow \{1, \dots, K\}, \\ y: E \rightarrow B \cap \{0, 1\}}} & \sum_{i \in V} c_V(i, x(i)) + \sum_{ij \in E} c_E(ij) y(ij) \\ \text{s.t.} & y(ij) = 0, \text{ if } x(i) = x(j) \\ & y(ij) = 1, \text{ if } x(i) \neq x(j) \end{aligned}$$

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$c_V, c_E$  : Semantic, edge costs

$x(i)$  : Semantic label of  $i$  in  $V$

$$y(ij) = \begin{cases} 0, & i, j \text{ belong to same instance} \\ 1, & i, j \text{ belong to different instance} \end{cases}$$

$B$  : Enforce valid clustering

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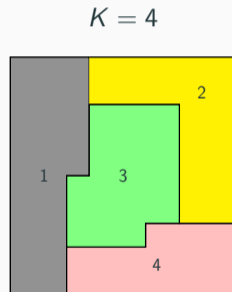
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# Asymmetric multiway cut (AMWC) - Kroeger 2014

AMWC on graph  $G = (V, E)$

$$\begin{aligned} \min_{\substack{x: V \rightarrow \{1, \dots, K\}, \\ y: E \rightarrow B \cap \{0, 1\}}} & \sum_{i \in V} c_V(i, x(i)) + \sum_{ij \in E} c_E(ij) y(ij) \\ \text{s.t.} & y(ij) = 0, \text{ if } x(i) = x(j) \notin P \\ & y(ij) = 1, \text{ if } x(i) \neq x(j) \end{aligned}$$

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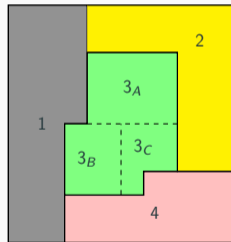
$B$  : Enforce valid clustering

$P \subset [K]$  : **Partitionable classes**

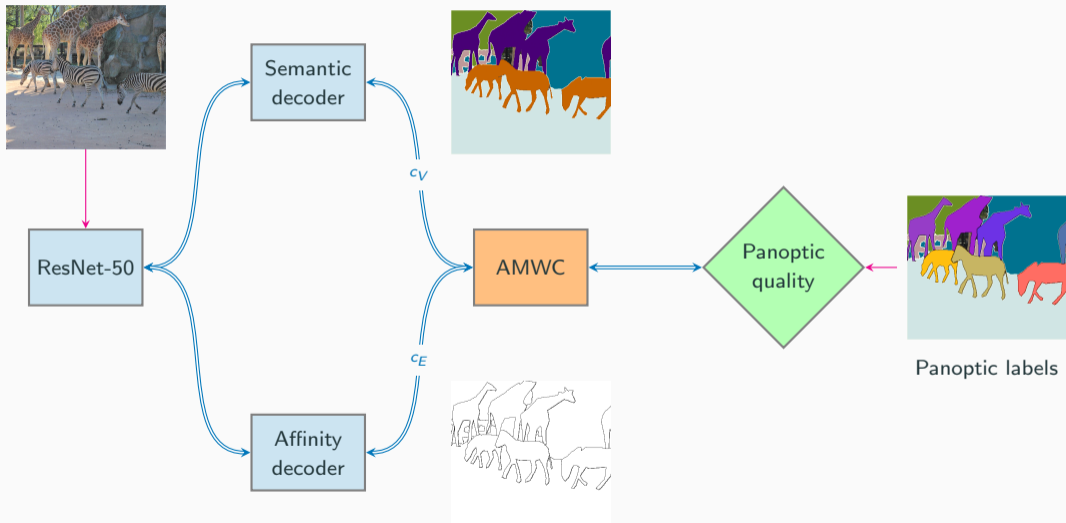
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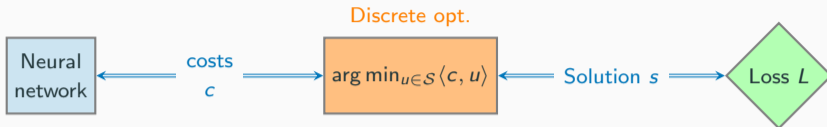
$K = 4, P = \{3\}$



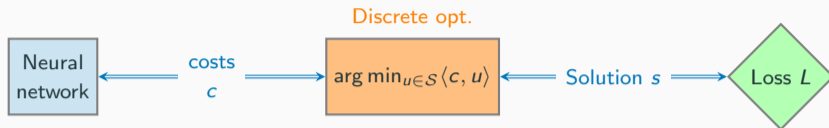
# Recap: our pipeline



# Gradient estimation through discrete optimization layers



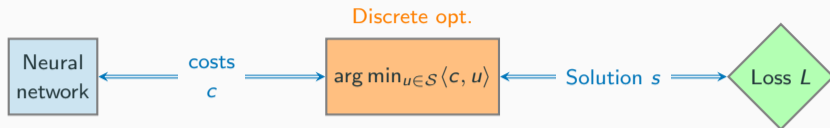
# Gradient estimation through discrete optimization layers



Build on the approach of Vlastelica 2019

$$\frac{\partial L_\lambda}{\partial c} = \frac{1}{\lambda} \left[ \mathbf{s}(c + \lambda \frac{\partial L}{\partial s}) - \mathbf{s}(c) \right]$$

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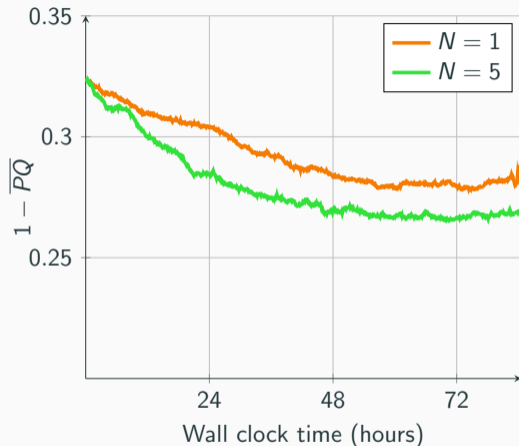
Our extension

$$\frac{\partial L_{avg}}{\partial c} = \frac{1}{N} \sum_i^N \frac{\partial L_{\lambda_i}}{\partial c}, \quad \lambda_i \sim \mathcal{U}(a, b)$$

- Averages gradients over multiple scales
- 3× faster convergence

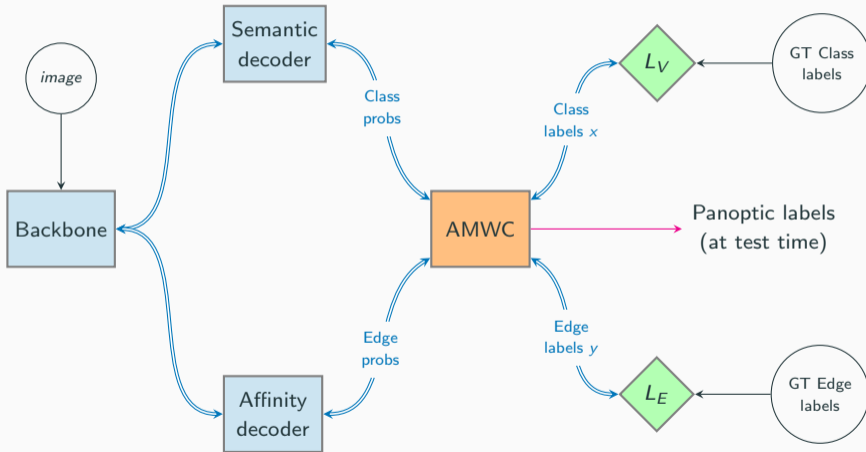


## Contribution 1: Improved gradient estimation



Training loss comparison ( $N = 5$ : our extension with **improved convergence**)

# Panoptic Segmentation: Naïve fully differentiable pipeline



## Naïve pipeline: Gradient estimation through AMWC

Perturb semantic, edge costs by respective **gradients**

$$\begin{aligned} \min_{\substack{x: V \rightarrow \{1, \dots, K\}, \\ y: E \rightarrow B \cap \{0, 1\}}} & \sum_i \left[ c_V(i, x(i)) + \frac{\partial L_V}{\partial x}((i, x(i))) \right] + \sum_{ij} \left[ c_E(ij) + \frac{\partial L_E}{\partial y}(ij) \right] y(ij) \\ \text{s.t.} & y(ij) = 0, \text{ if } x(i) = x(j) \notin P \\ & y(ij) = 1, \text{ if } x(i) \neq x(j) \end{aligned}$$

# Panoptic Segmentation: Naïve fully differentiable pipeline

Does not perform well:

- Edge misclassifications are **not** equally important
- At test-time we care about pixel labels not edge labels
- Need to optimize test-time metric of panoptic quality (PQ)



Edge labels: **ground-truth**, **prediction**, **correct predictions**

## Contribution 2: Optimize panoptic quality surrogate

Approximate non-differentiable panoptic quality metric

$$PQ = \frac{\sum_{(p,g) \in TP} IoU(p,g)}{|TP| + 0.5(|FP| + |FN|)}$$

by

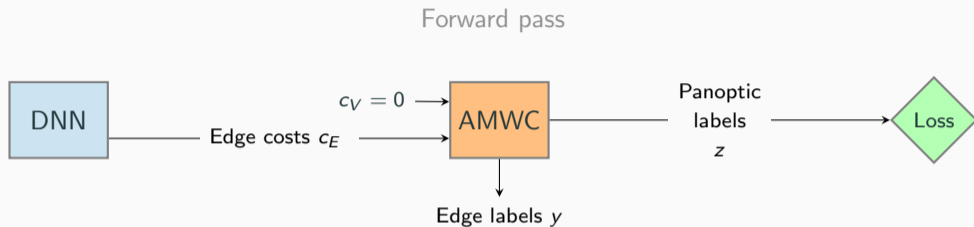
$$\overline{PQ} = \frac{\sum_{(p,g) \in \overline{TP}} h(IoU(p,g)) \sigma(p) IoU(p,g)}{\sum_{(p,g) \in \overline{TP}} h(IoU(p,g)) \sigma(p) + 0.5\{\sum_{p \in \overline{FP}} \sigma(p) + |\overline{FN}|\}}$$

where

$h(\cdot)$ : Soft-thresholding

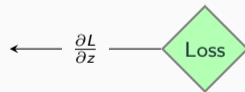
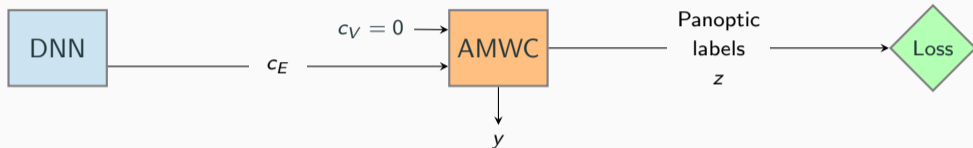
$\sigma(p)$ : Foreground probability (from mask area)

## Contribution 3: Backprop with loss on panoptic labels ( $K = 1$ )



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Forward pass

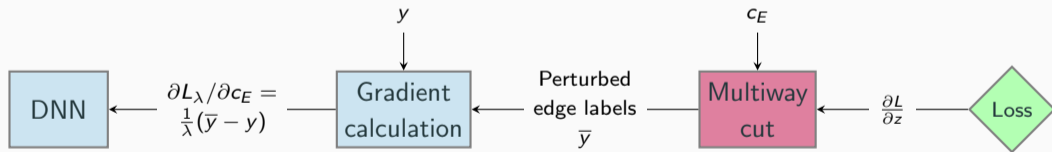
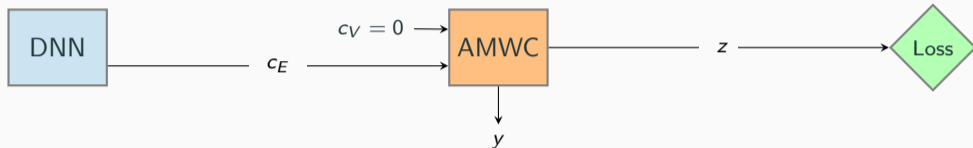


Backward pass

*Ignored semantic costs  $c_V$  for brevity*

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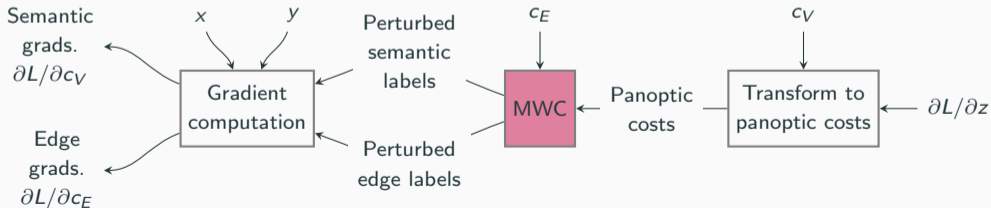
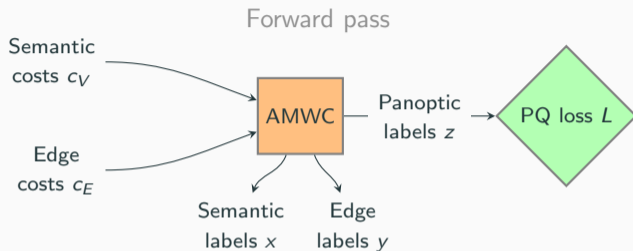


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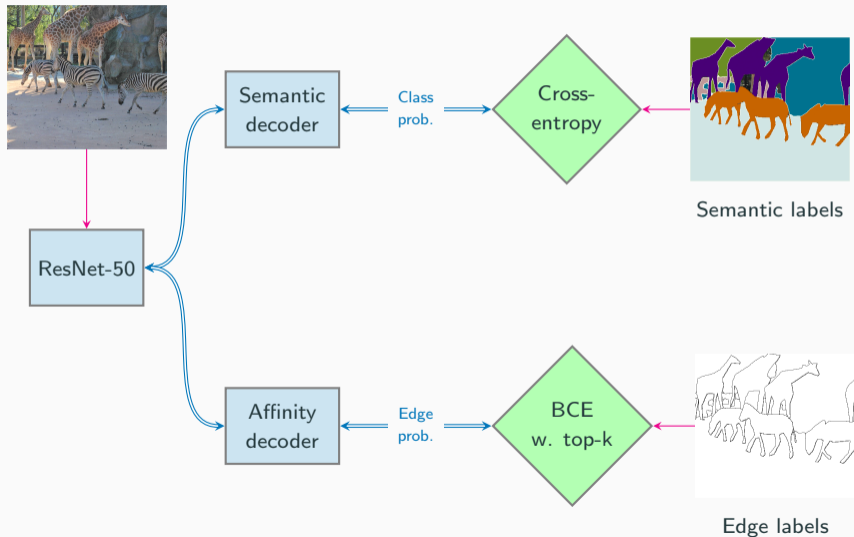


## Contribution 3: Full backprop ( $K \geq 1$ ) with loss on panoptic labels



Backward pass with transformation to panoptic label space

# Baseline: train by 'usual' losses







# Results






- Outperform all comparable approaches
- Sometimes, even with a disadvantage (e.g. smaller backbone)



Methods	Architecture	Hyperparameters		E-to-E	Opt. PQ	Panoptic qual.	
		Train	Eval			Citysc.	COCO
MaxDeepLab						-	49.3
EfficientPS						63.9	-
AxialDeepLab						63.9	41.8
UPNet						59.3	42.5
SSAP						61.1	36.5
SMW						59.3	-
PanopticDeepLab						60.2	35.1
Our baseline						58.5	34.3
<b>Our fully differentiable</b>						<b>62.1</b>	<b>38.4</b>

# Summary

- Simple and fully differentiable pipeline for panoptic segmentation
- Improved gradient estimation through discrete optimization problems
- Optimize panoptic quality differentiable surrogate
- Transformation to MWC in backward pass to compute gradients
- First large-scale study of backpropagation through heuristic optimization solvers
- *Shortcoming*: Inference time of around 2s per image
- **Code available at:** [github.com/aabbas90/COPS](https://github.com/aabbas90/COPS)

-  Calinescu, Gruia (2008). “Multiway Cut”. In: *Encyclopedia of Algorithms*. Ed. by Ming-Yang Kao. Boston, MA: Springer US, pp. 567–569. ISBN: 978-0-387-30162-4. DOI: 10.1007/978-0-387-30162-4\_253. URL: [https://doi.org/10.1007/978-0-387-30162-4\\_253](https://doi.org/10.1007/978-0-387-30162-4_253).
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